

Foreshocks are not predictive of future earthquake size

Morgan Page, Karen Felzer, and Andrew Michael
U.S. Geological Survey



Foreshocks are not predictive of future earthquake size

(but nevertheless contain quite a bit of predictive power)

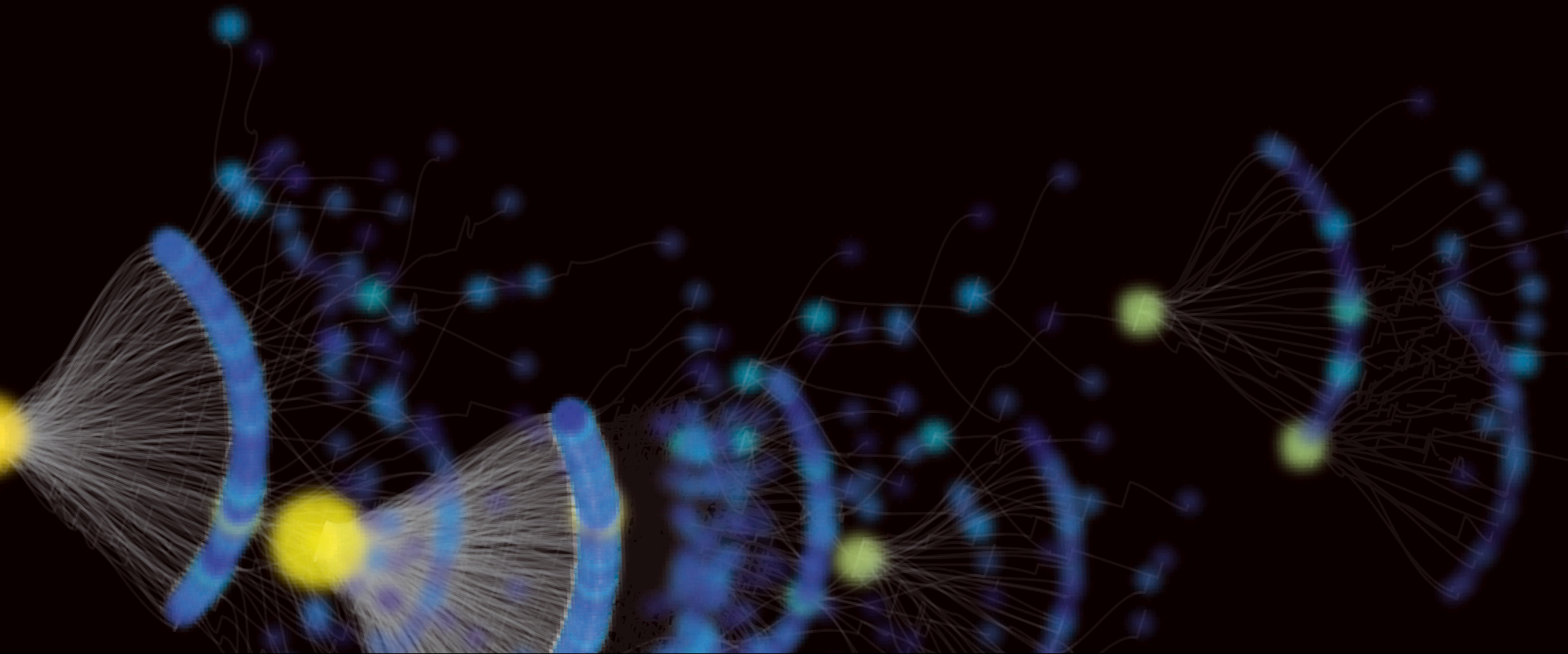
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The Cascade Model

Small and large earthquakes nucleate in the same way

There is some probability that a given earthquake will grow large,
but size is unpredictable ahead of time

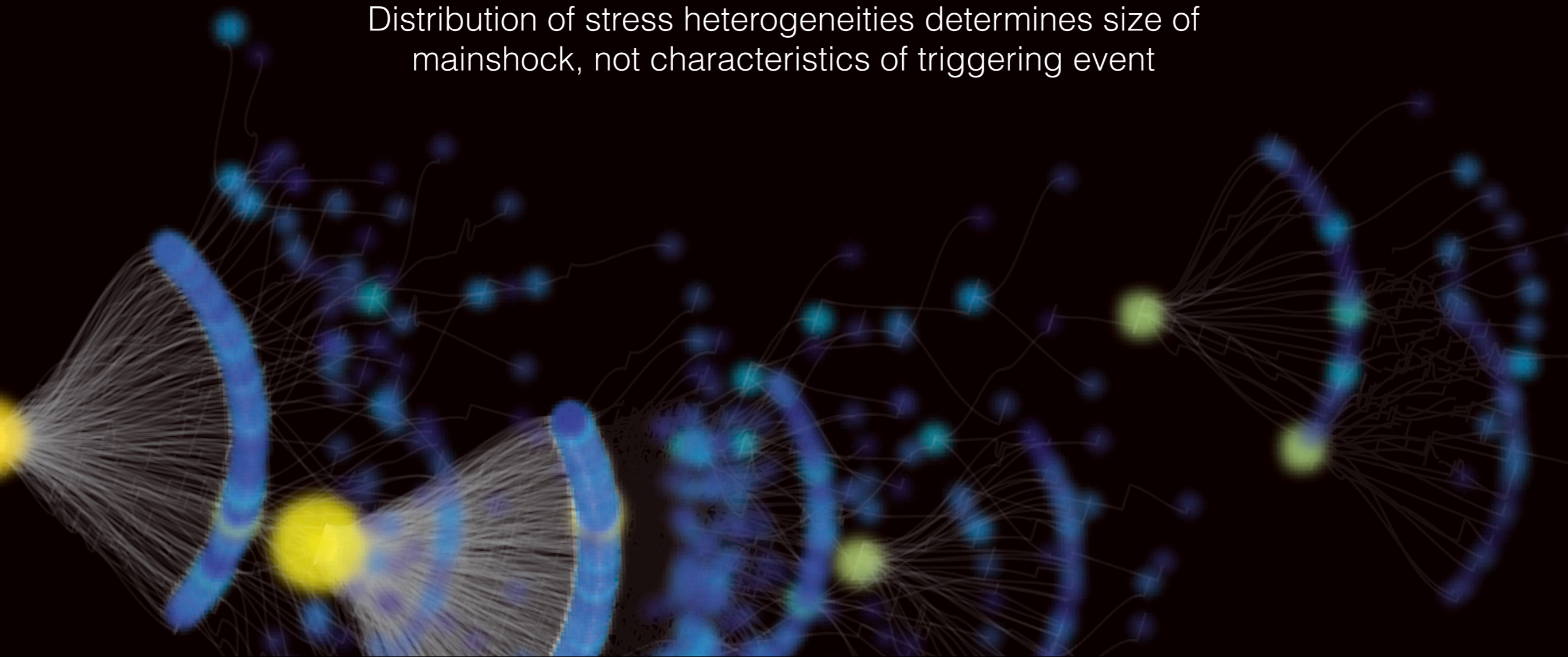


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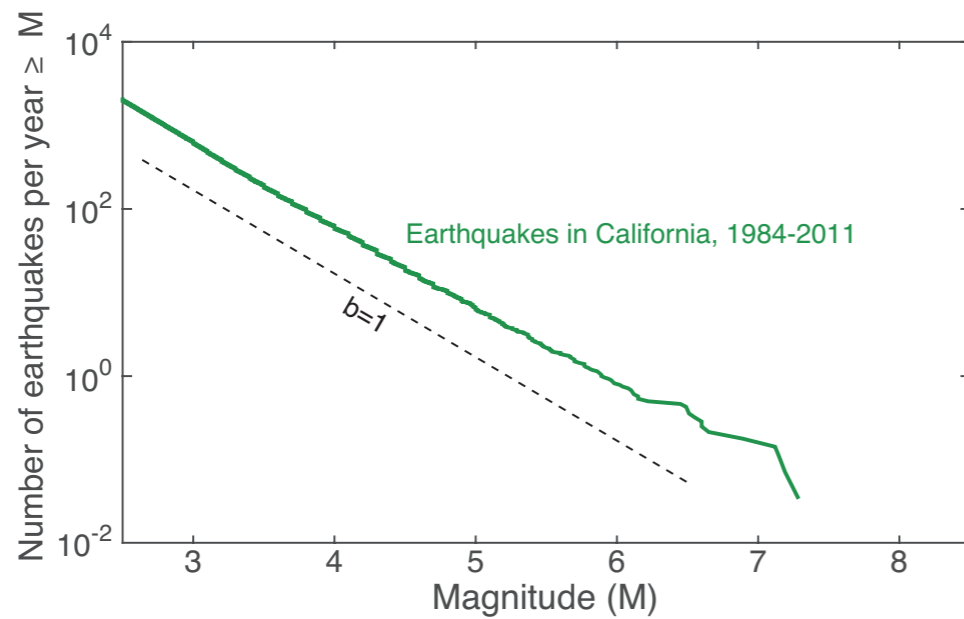
There is some probability that a given earthquake will grow large,
but size is unpredictable ahead of time

Distribution of stress heterogeneities determines size of
mainshock, not characteristics of triggering event



The Basics of Earthquake Forecasting

The Statistical Seismologist's Approach

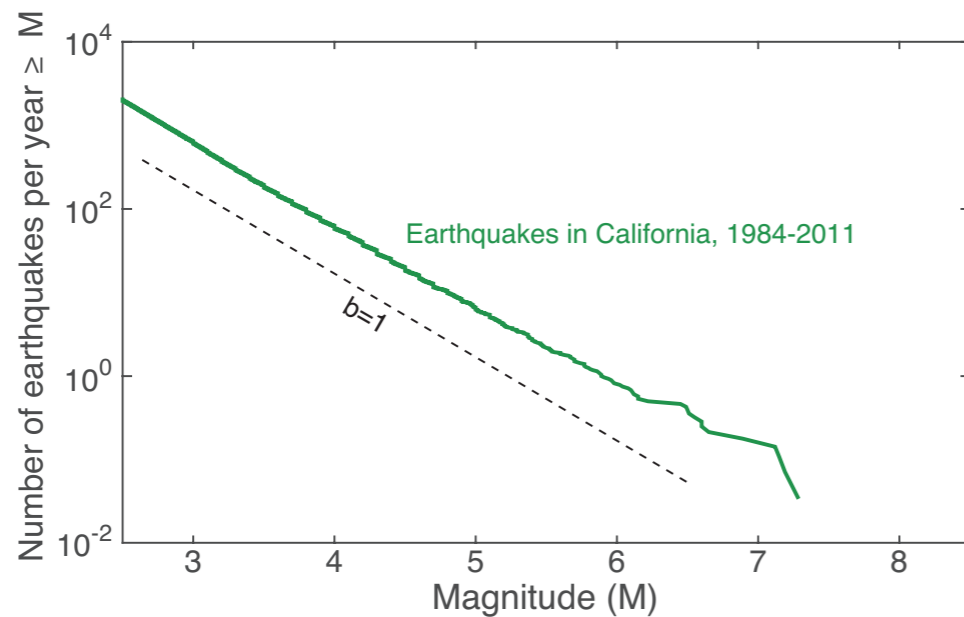


Gutenberg-Richter Magnitude Scaling

$$N(M) \propto 10^{(a-bM)}$$

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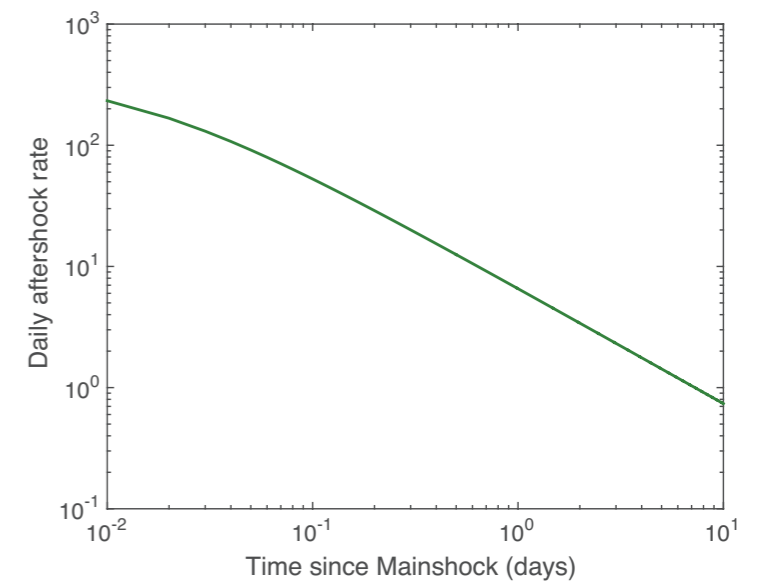


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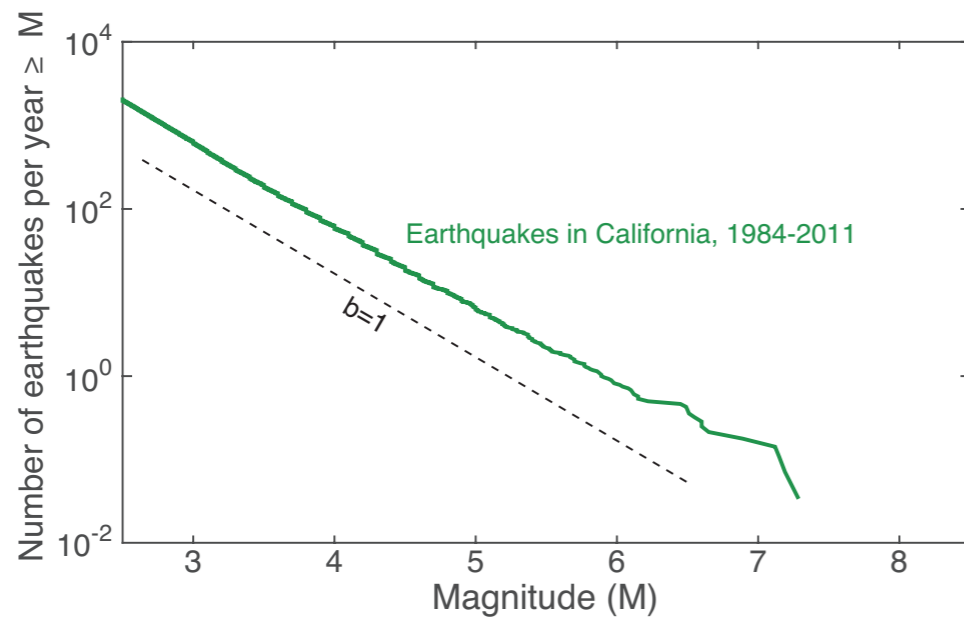
Omori
Decay of
Aftershock
Rate

$$\lambda(t) = (t + c)^{-p}$$



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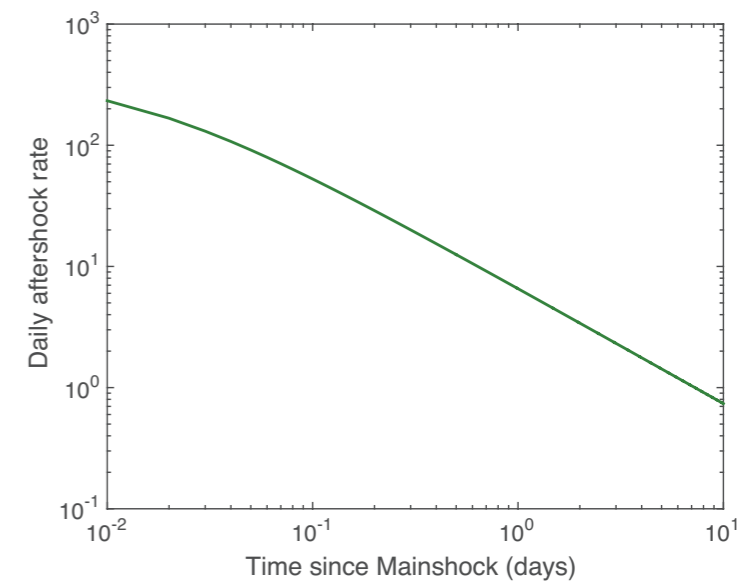


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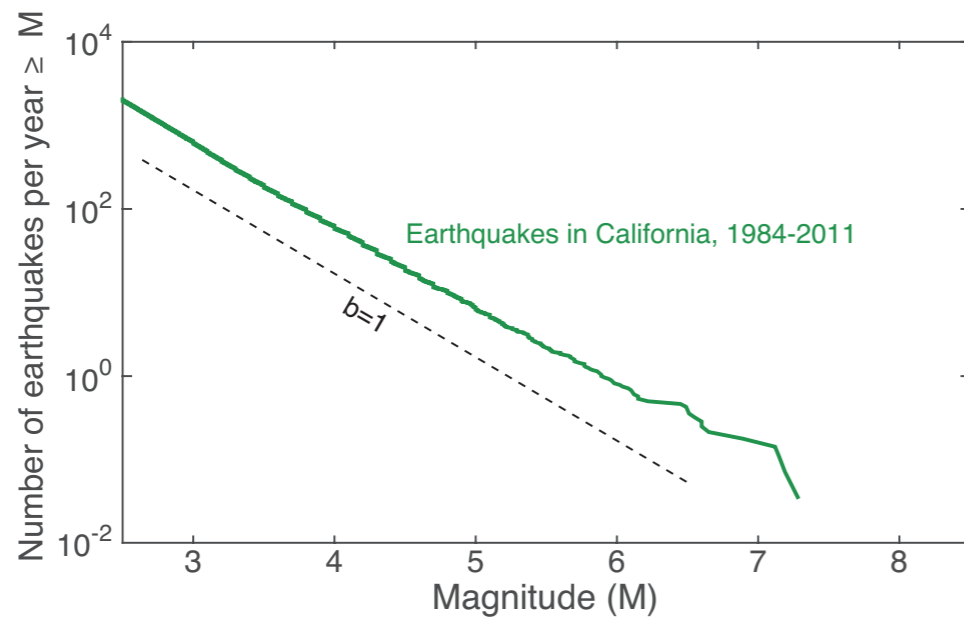


Big earthquakes trigger more aftershocks

$$\lambda \propto 10^{b(M)}$$

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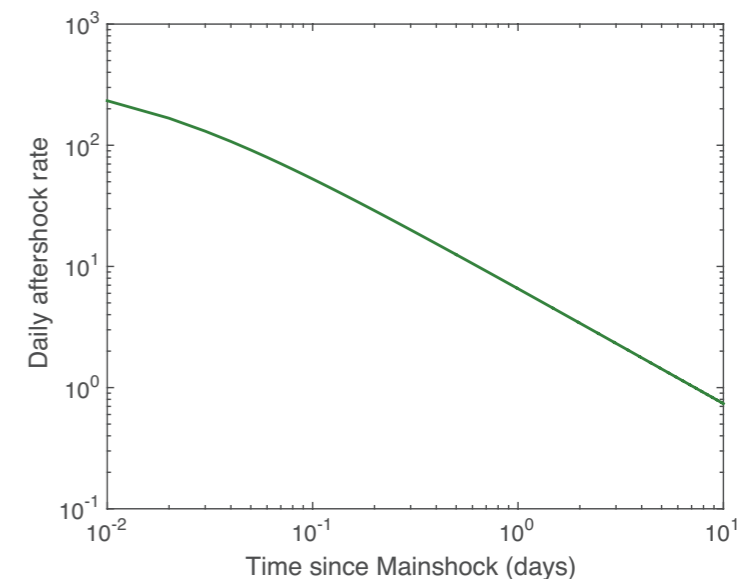


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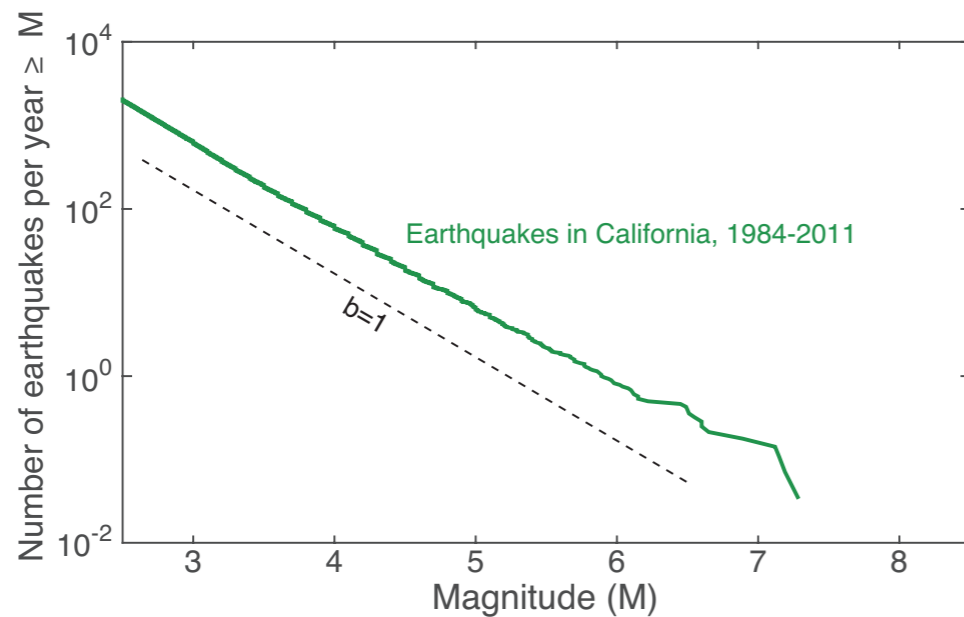
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Aftershock rates decay with distance from the mainshock

$$p(r) \propto N(r) (r^2 + d^2)^{-\gamma/2}$$

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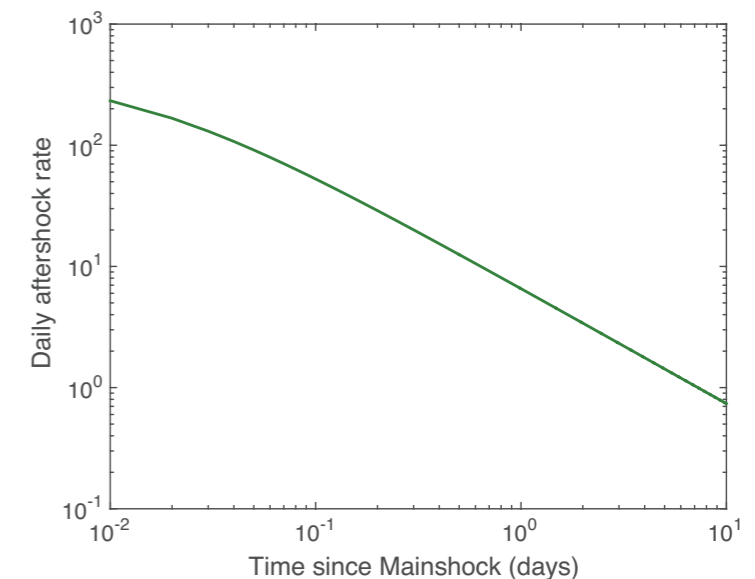


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These scaling laws are used in short-term forecasting models like ETAS (Ogata, 1988) and STEP (Gerstenberger et al., 2005)

Alternatives to cascade model

Pre-slip

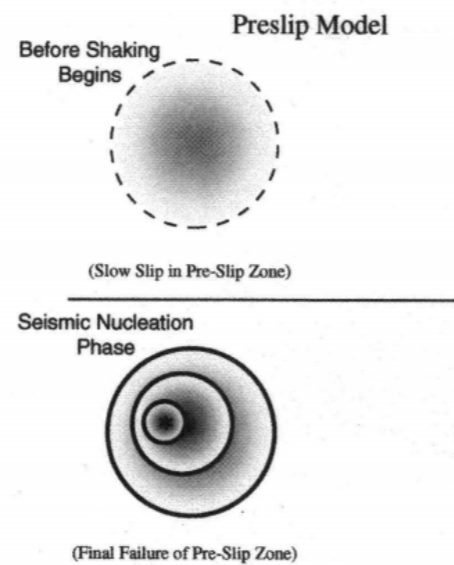


figure from Vidale et al. (2001)

Foreshocks result from aseismic slip in the nucleation zone of future large earthquake

Alternatives to cascade model

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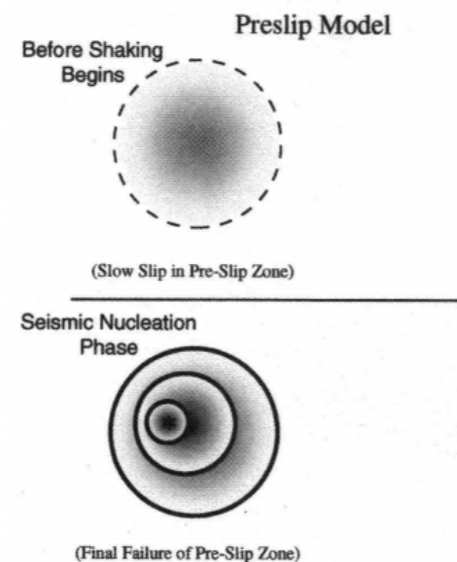
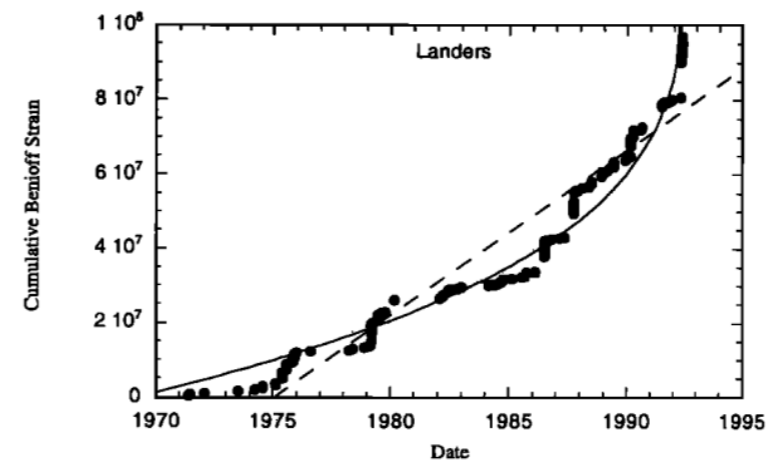


figure from Vidale et al. (2001)

Foreshocks result from aseismic slip in the nucleation zone of future large earthquake

Accelerating Moment Release (AMR)



Bowman et al. (1998)

Hardebeck et al. (2008) showed the hypothesis was statistically insignificant

(ETAS catalogs can produce just as much apparent acceleration)

Alternatives to cascade model

Pre-slip

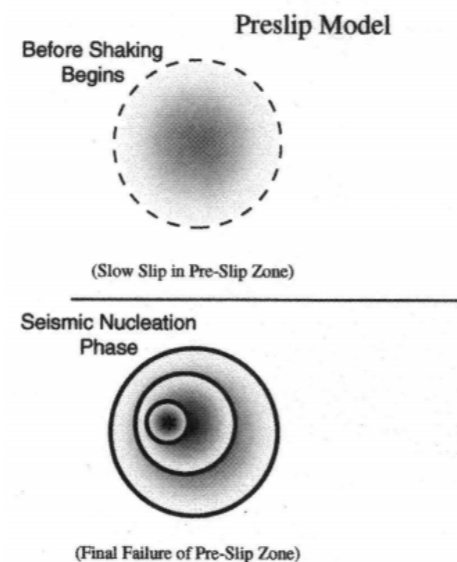
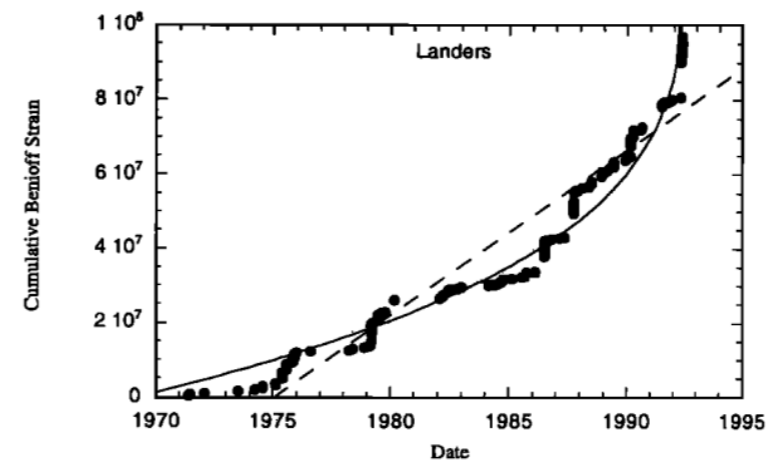


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Foreshocks result from aseismic slip in the nucleation zone of future large earthquake



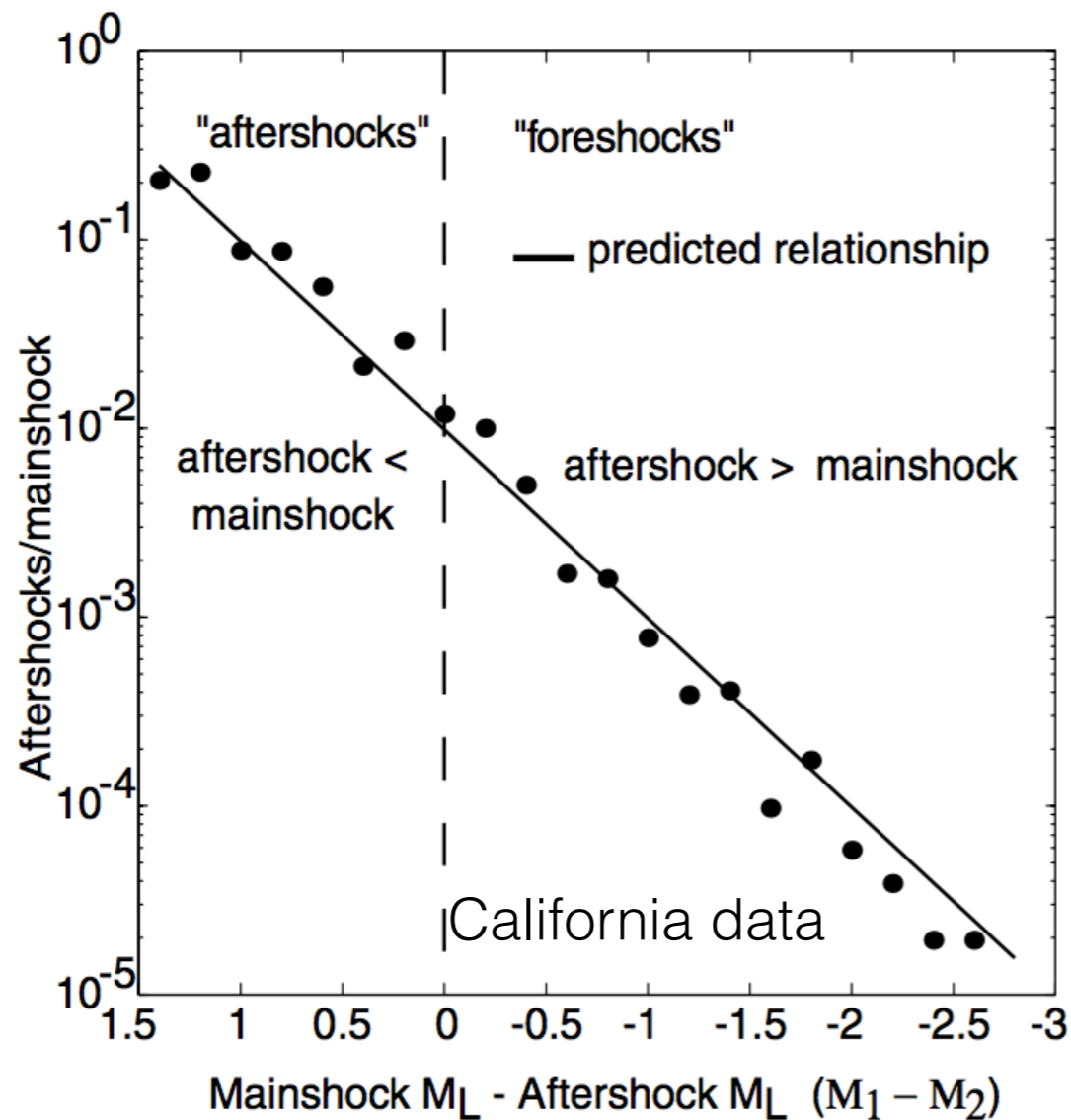
Bowman et al. (1998)

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Unlike cascade model, these models hypothesize that foreshocks are “different” from other earthquakes and are predictive of future earthquake size

Cascade Model Predictions

The foreshock rate and the aftershock rate follow the same trend ✓

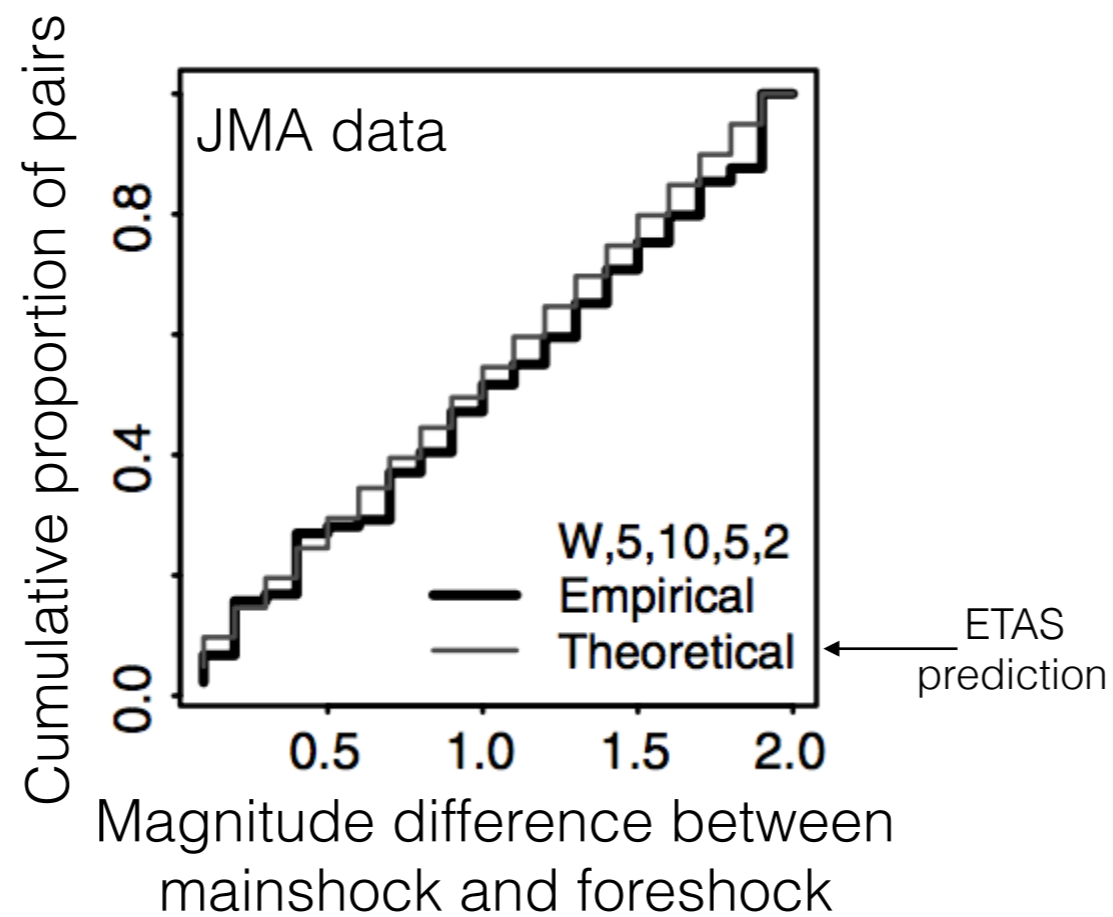


Given the aftershock rate, you can predict the foreshock rate, suggesting they represent the same process

Felzer et al. (2004)

Cascade Model Predictions

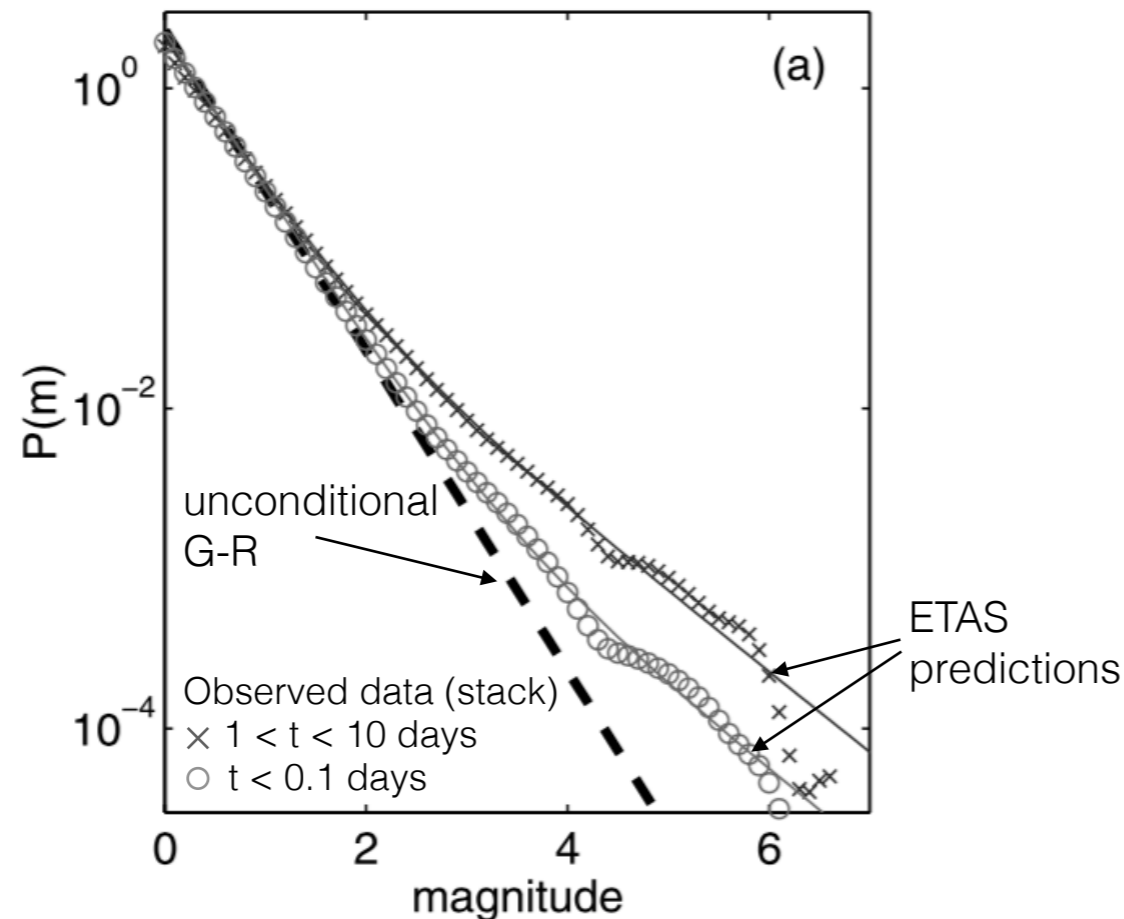
The magnitude distribution of foreshocks is uniform ✓



Smythe et al. (2011)

Cascade Model Predictions

Apparent decrease in b-value prior to mainshocks ✓

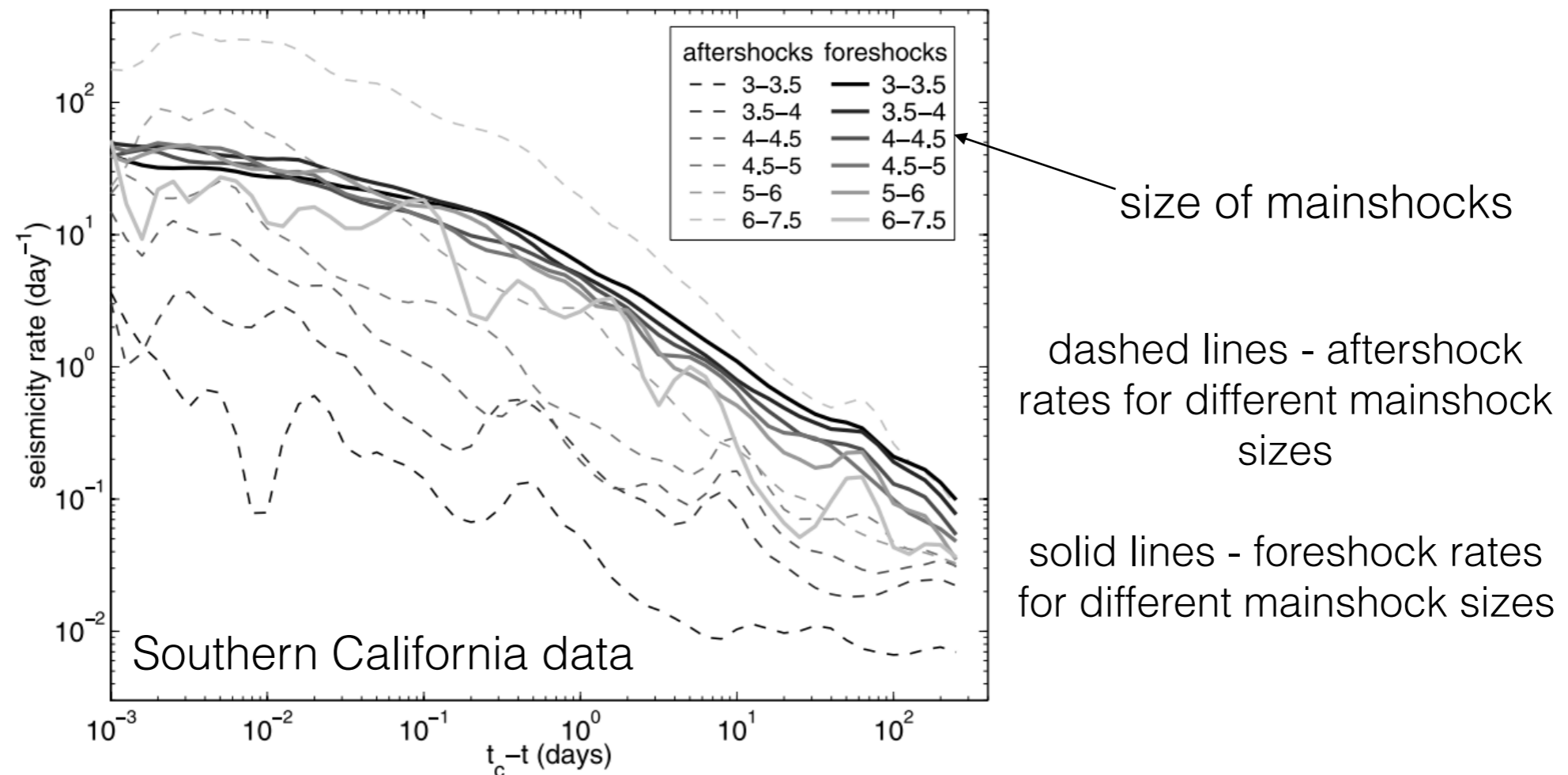


Larger earthquakes are more likely to trigger an earthquake than smaller earthquakes (because they trigger more earthquakes), so the *conditional* magnitude distribution prior to stacked “mainshocks” has a lower b-value at higher magnitudes

Helmstetter et al. (2003)

Cascade Model Predictions

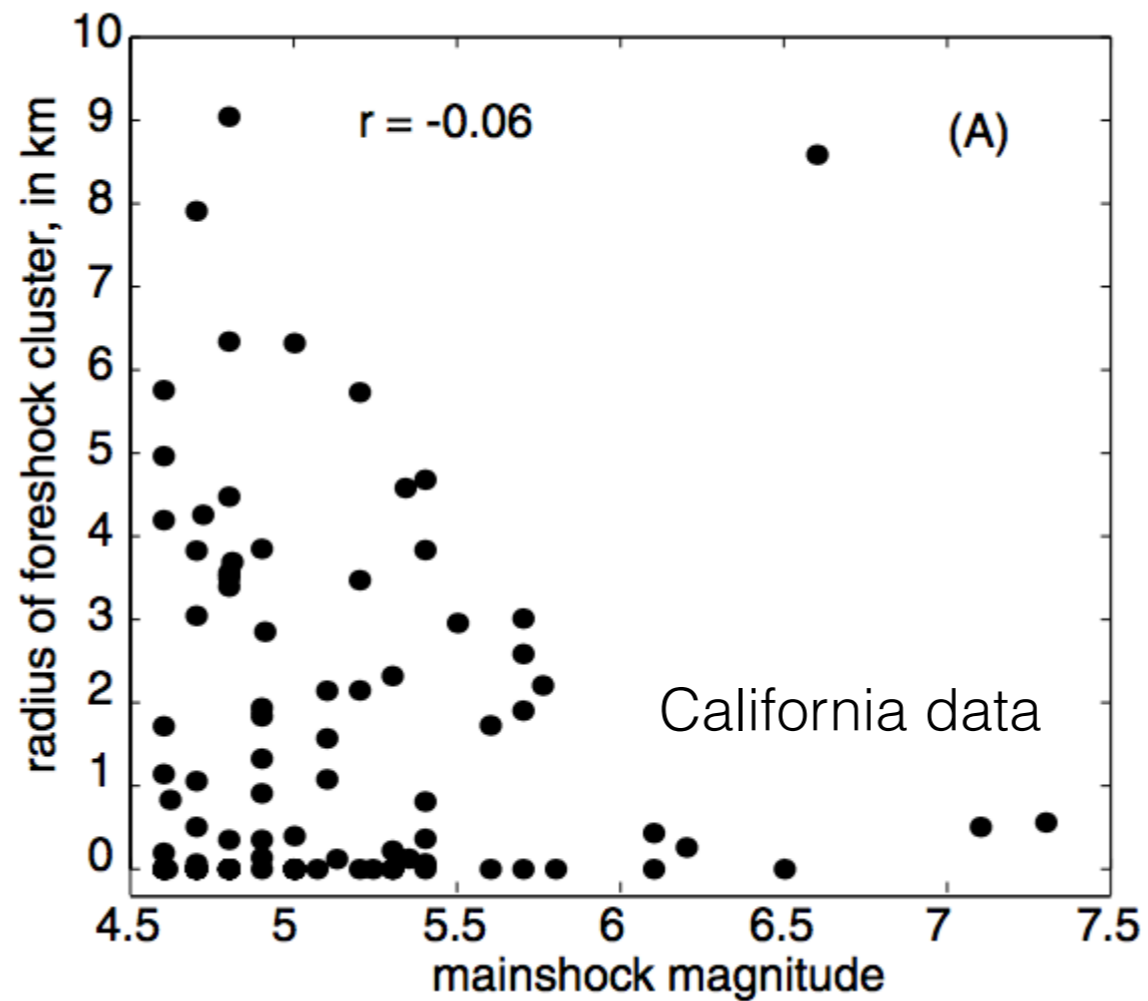
No significant correlation between number of foreshocks and mainshock size ✓



Helmstetter and Sornette (2003)

Cascade Model Predictions

No significant correlation between foreshock area and mainshock size



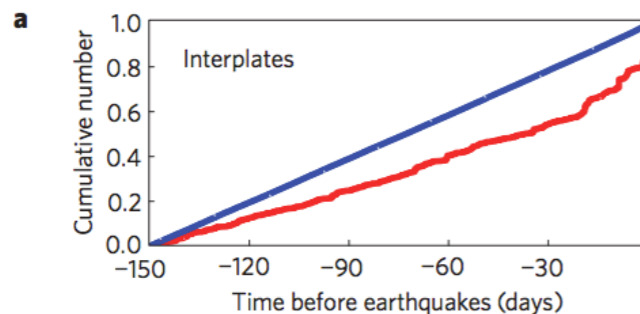
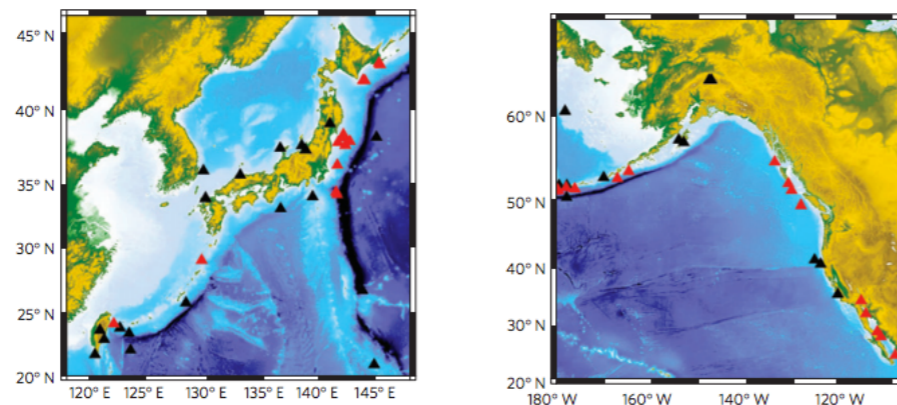
Recent Challenges to the Cascade Model

Bouchon et al. (2013)



The long precursory phase of most large interplate earthquakes

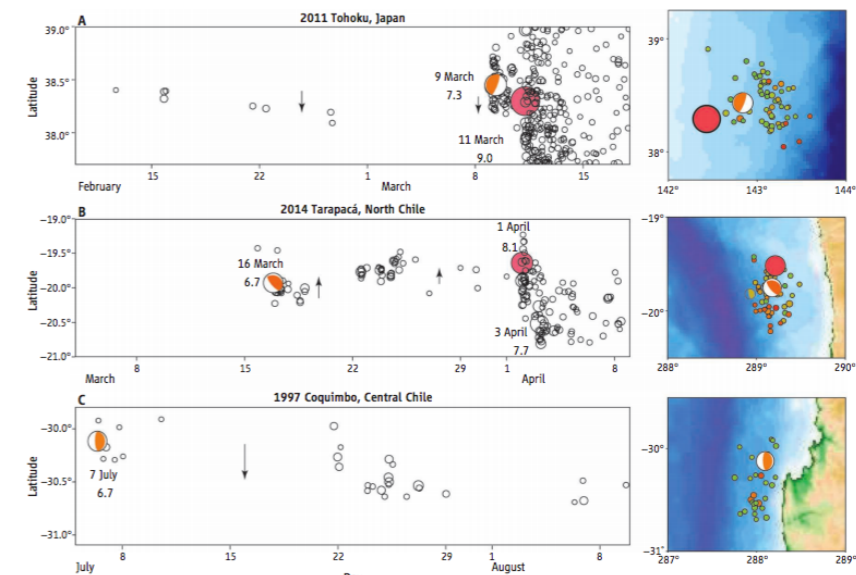
Michel Bouchon^{1*}, Virginie Durand^{1,2*}, David Marsan², Hayrullah Karabulut³ and Jean Schmittbuhl⁴



Brodsky and Lay (2014)

Recognizing Foreshocks from the 1 April 2014 Chile Earthquake

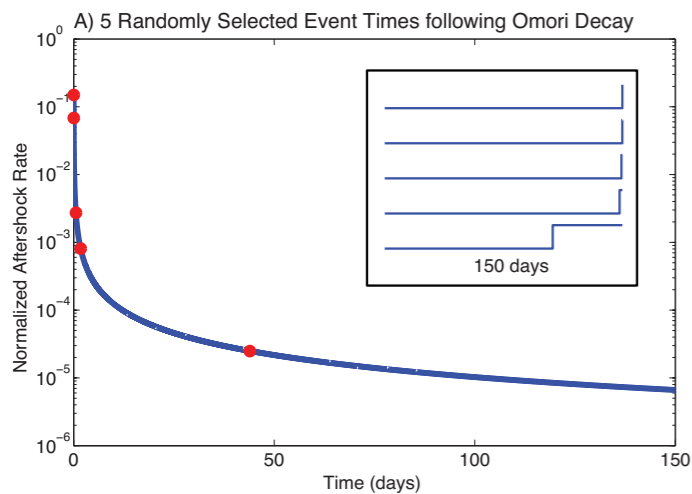
Emily E. Brodsky and Thorne Lay



Could slow slip or foreshock migration be used to forecast impending large earthquakes?

Inverse Omori Acceleration

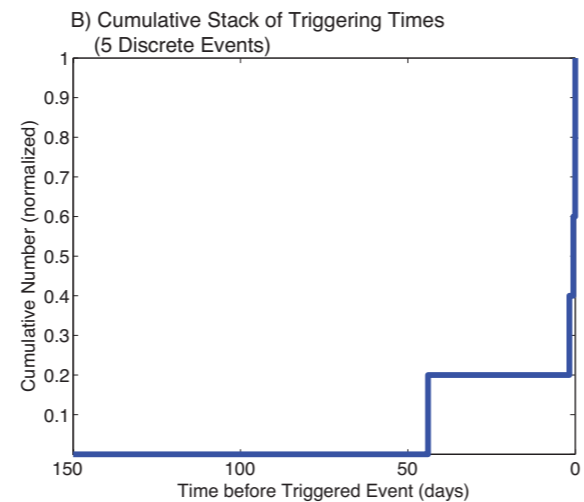
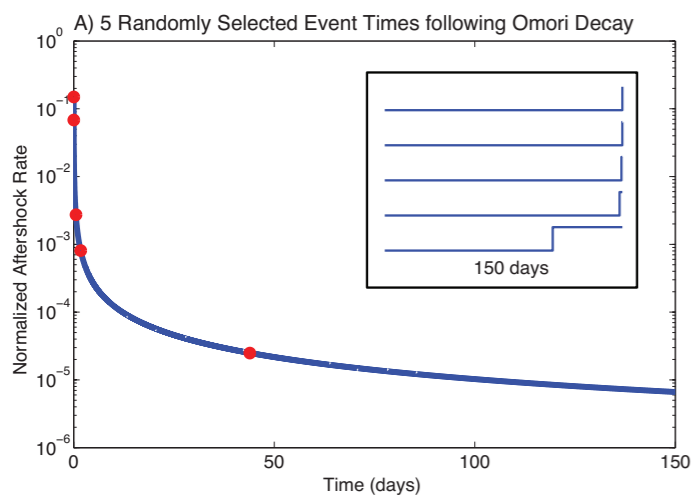
The Omori Law predicts “acceleration” in stacked foreshock sequences



randomly
selected times
from Omori rate
distribution

Inverse Omori Acceleration

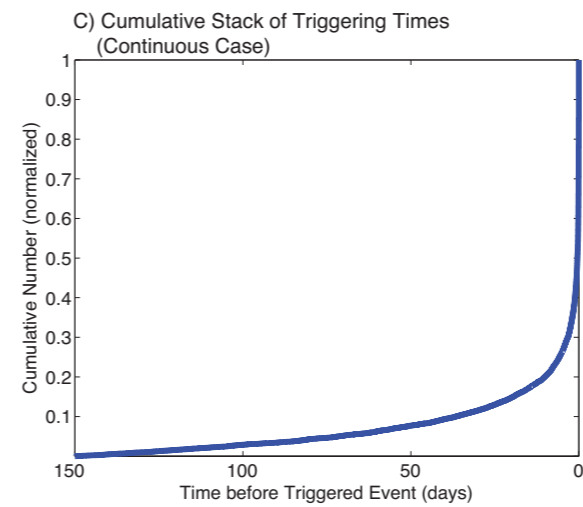
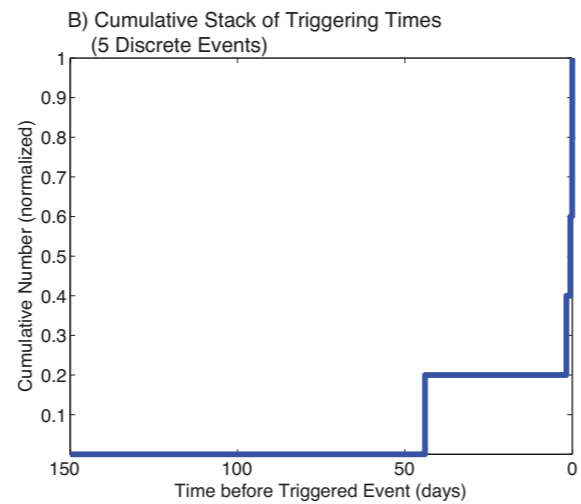
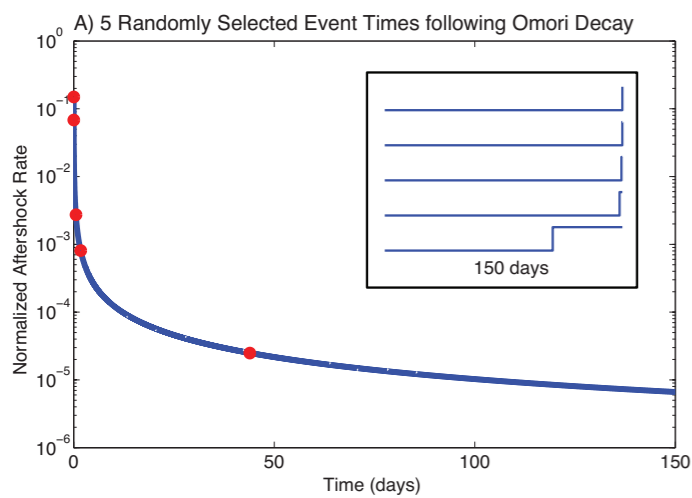
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cumulative
stack of these
triggering
times

Inverse Omori Acceleration

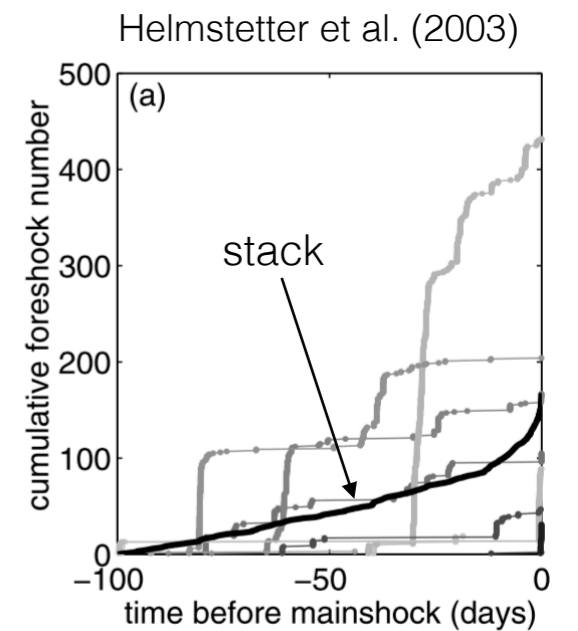
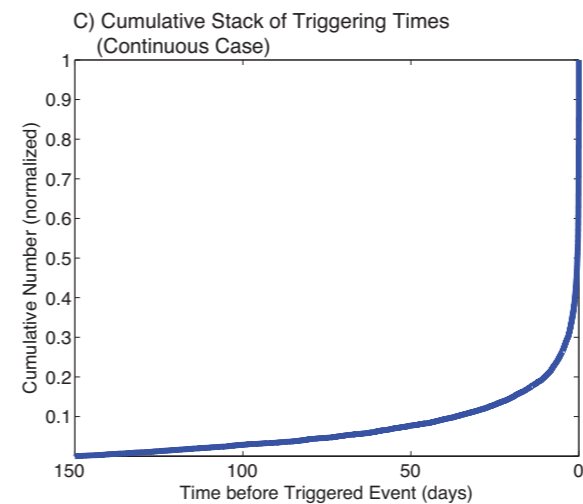
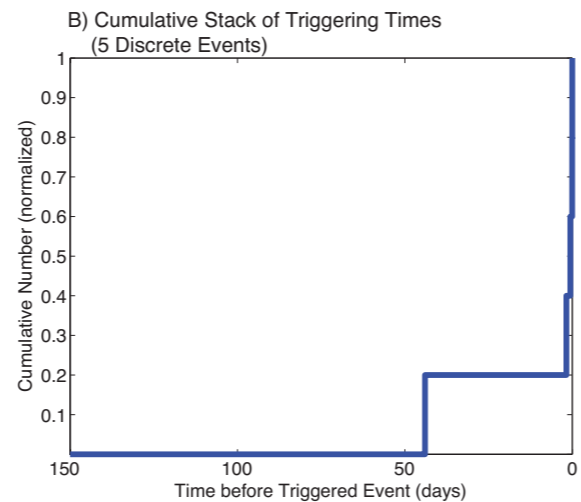
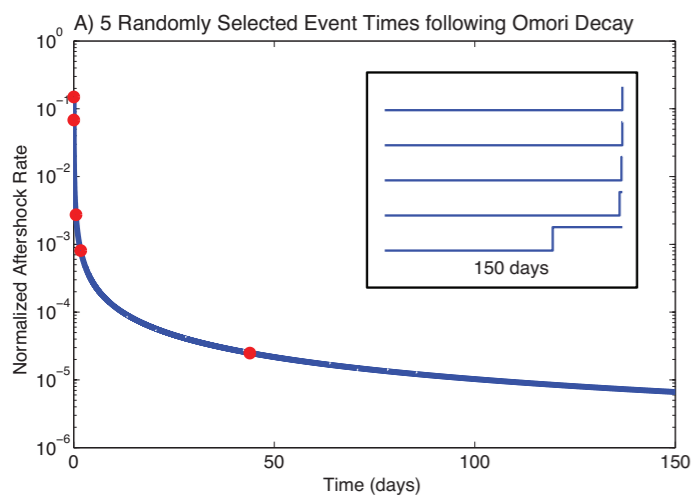
The Omori Law predicts “acceleration” in stacked foreshock sequences



continuous
version

Inverse Omori Acceleration

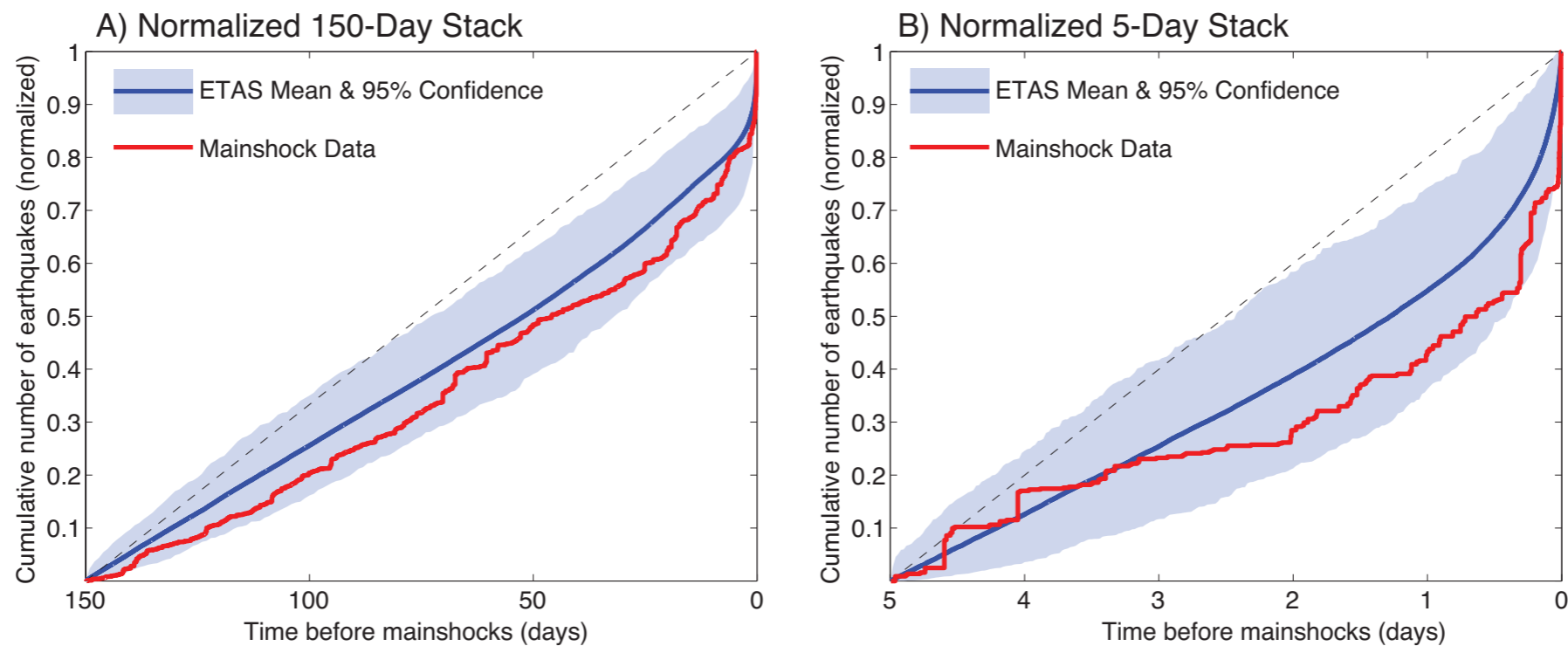
The Omori Law predicts “acceleration” in stacked foreshock sequences



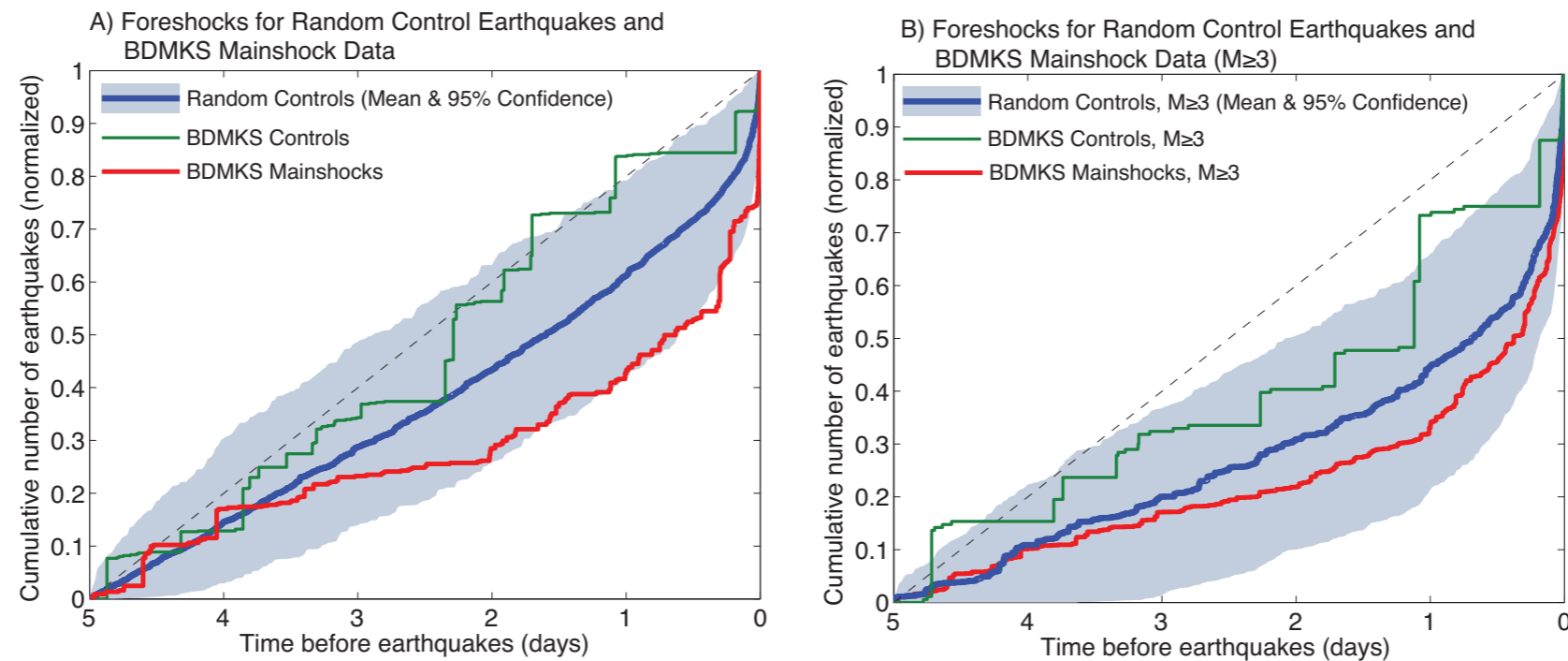
real data
example

Inverse Omori Acceleration

ETAS models can match the acceleration seen in Bouchon et al. (2014) dataset

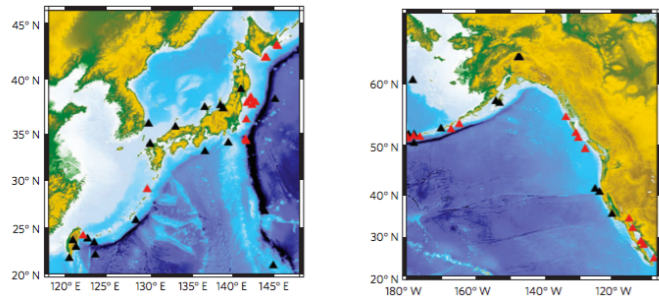


The cascade model predicts that the same amount of inverse Omori acceleration should be seen before earthquakes of any size



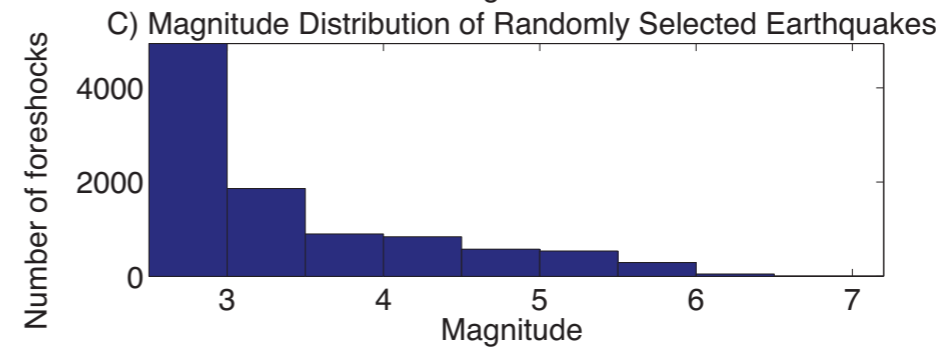
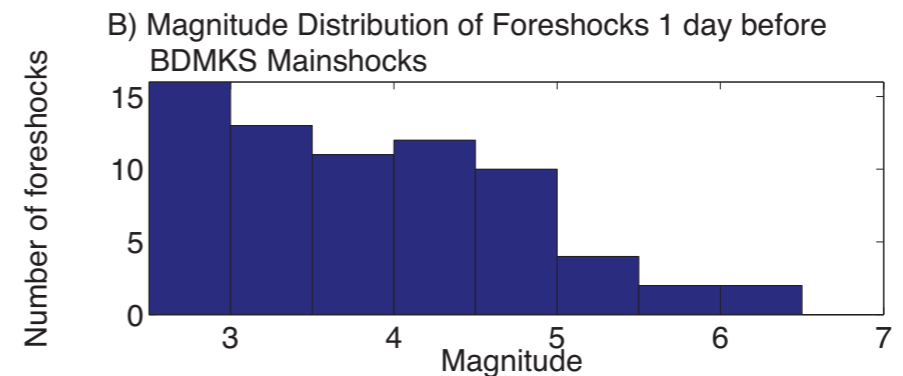
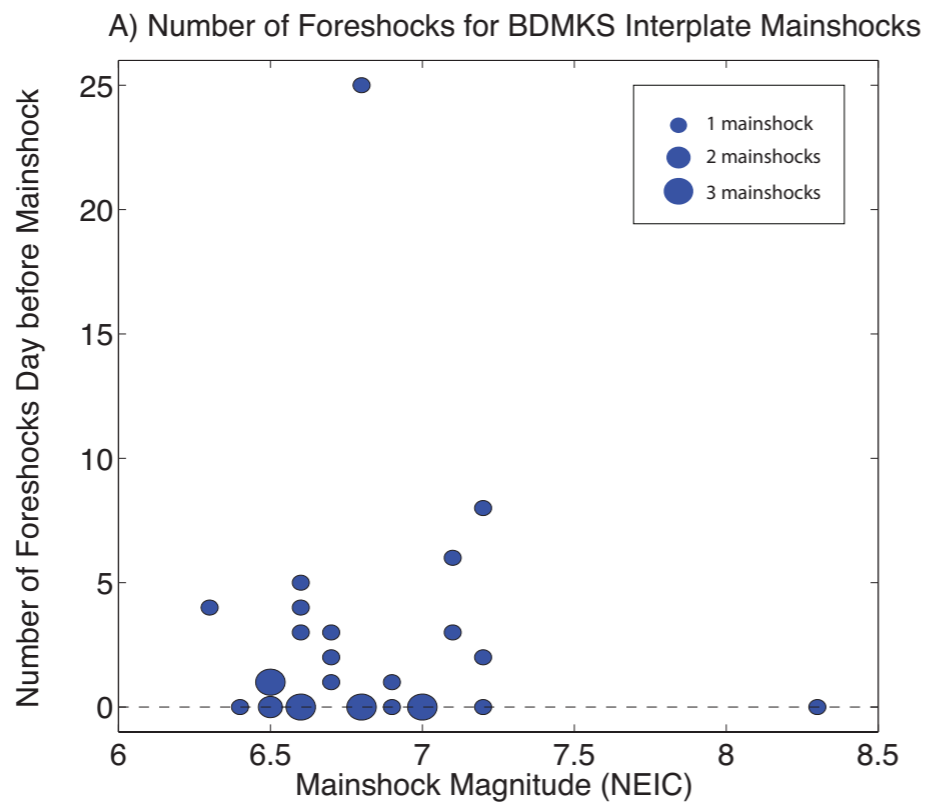
Indeed, the acceleration before small earthquakes is similar (if you correct for completeness problems in the Bouchon et al. (2014) dataset)

Bouchon et al. (2013) dataset

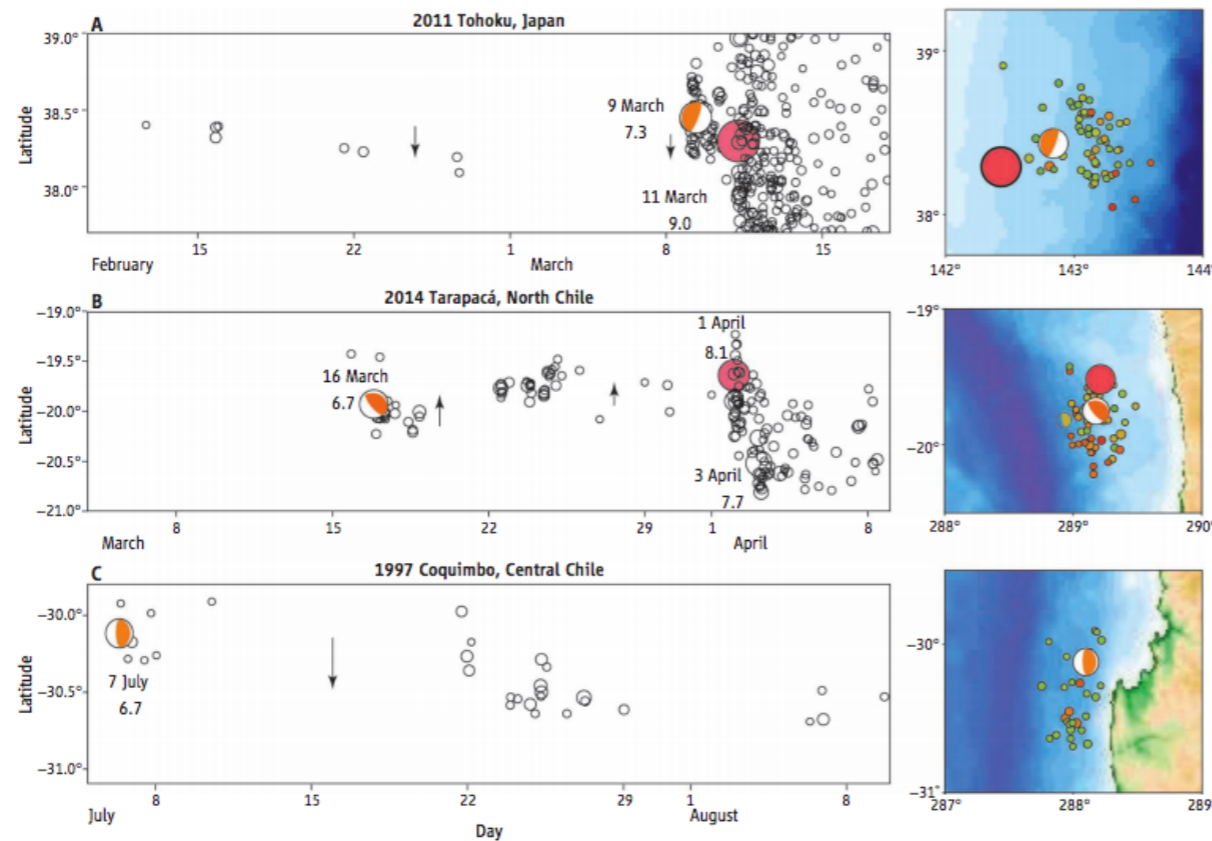


The number of foreshocks does not scale with mainshock size ...

...and the foreshock magnitude distribution is approximately uniform, not G-R distributed.



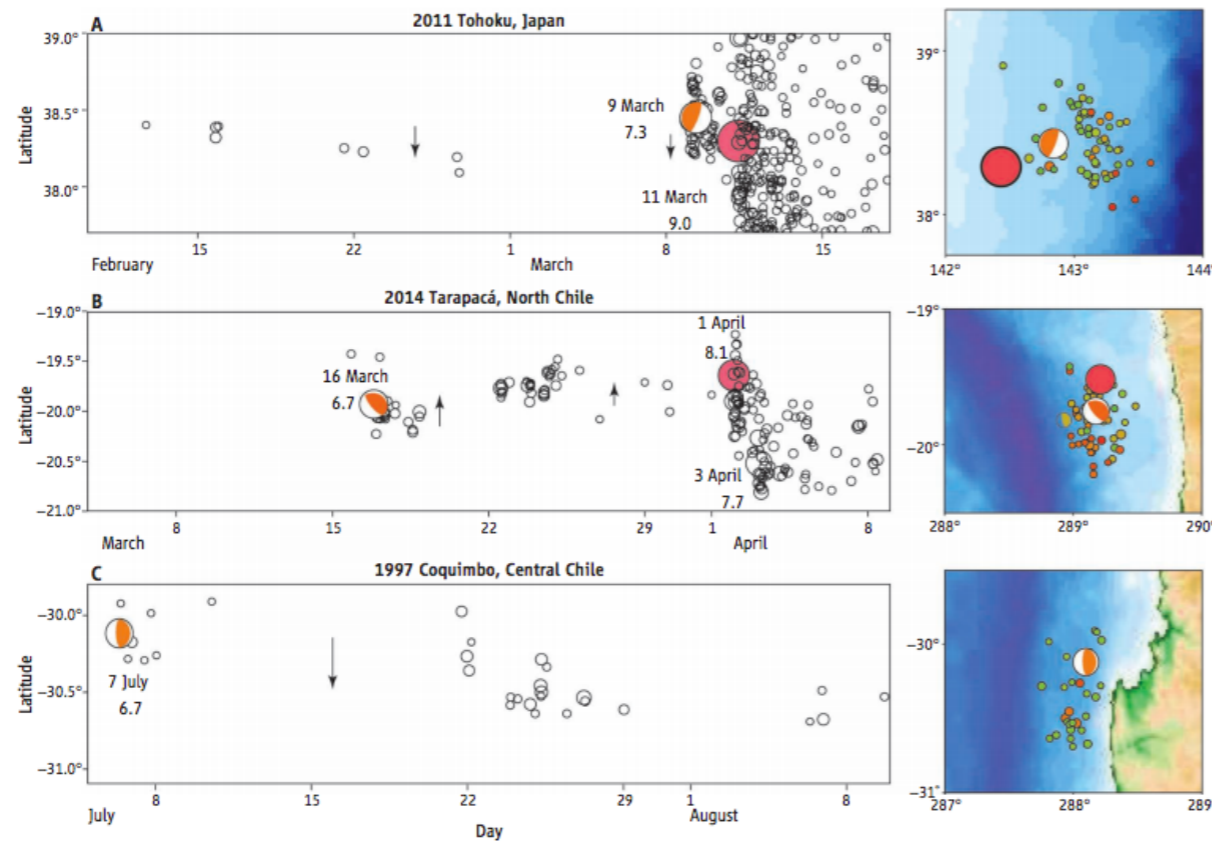
Slow slip & seismicity migration may indeed happen, but does that imply predictability for mainshock size?



A wealth of data supporting foreshock scaling laws suggests no.

Brodsky and Lay (2014)

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Brodsky and Lay (2014)

A wealth of data supporting foreshock scaling laws suggests no.

Foreshocks do contain predictive power, but not about the size of the mainshock.

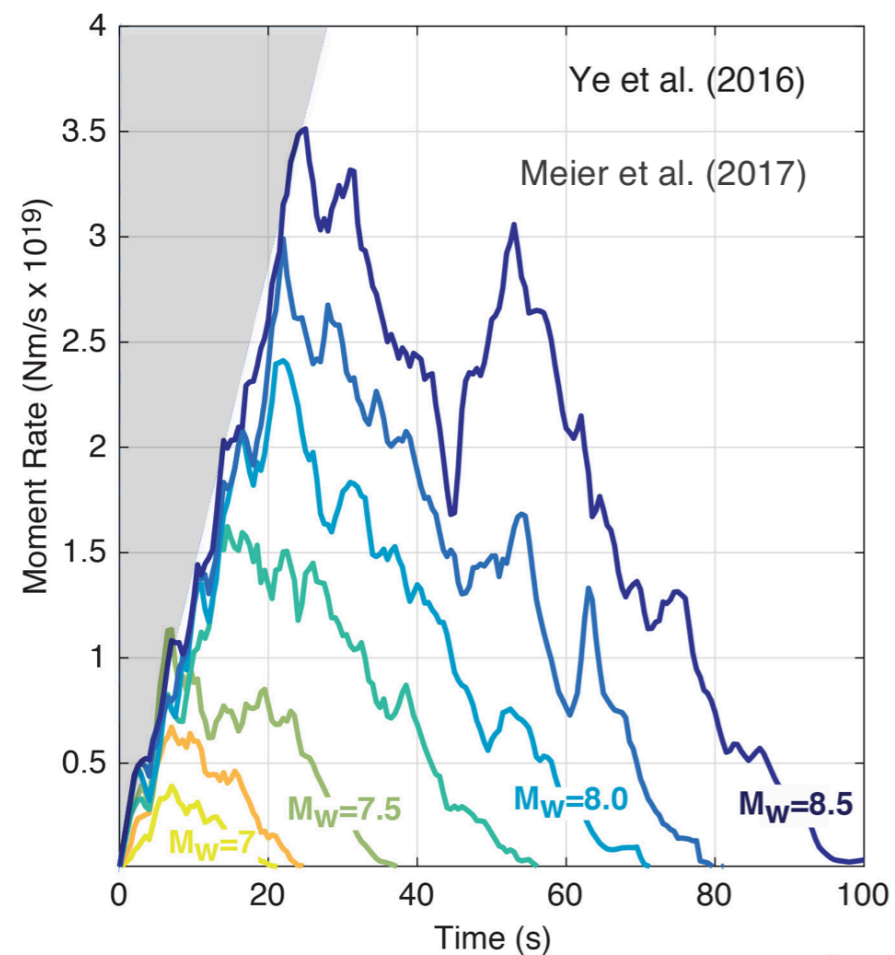
Foreshocks are not predictive of mainshock size

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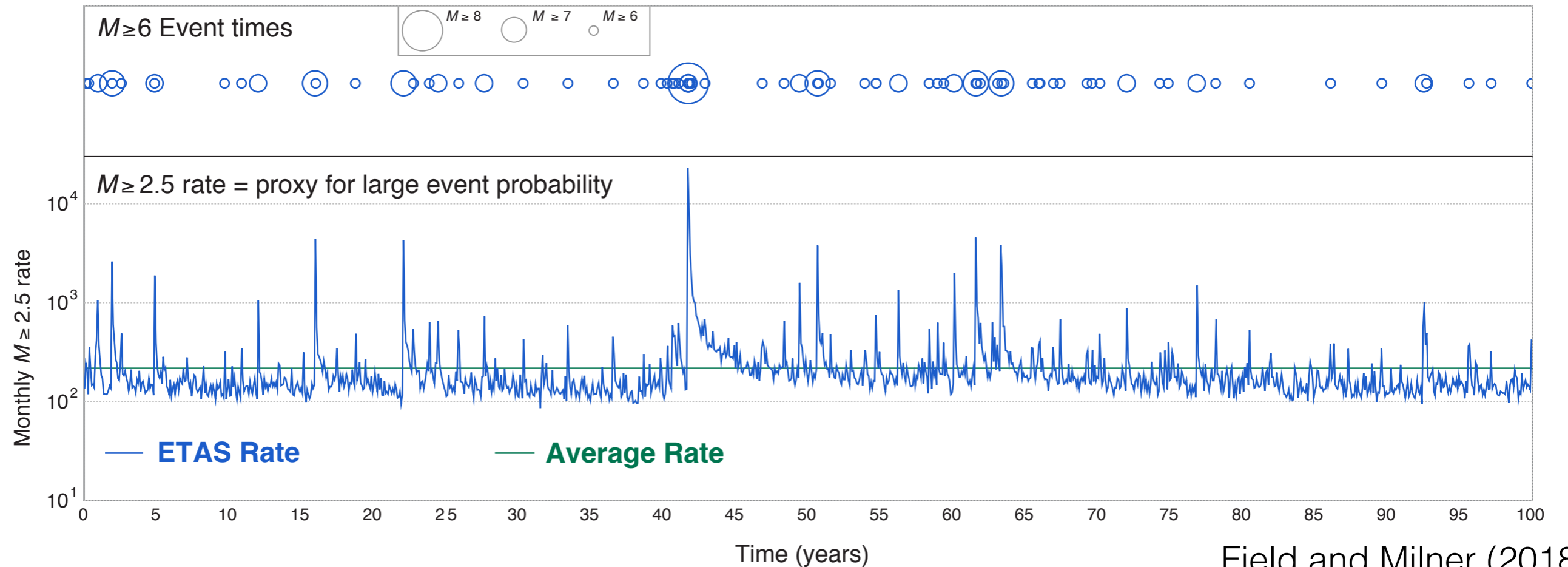
The hidden simplicity of subduction megathrust earthquakes

M.-A. Meier,* J. P. Ampuero, T. H. Heaton



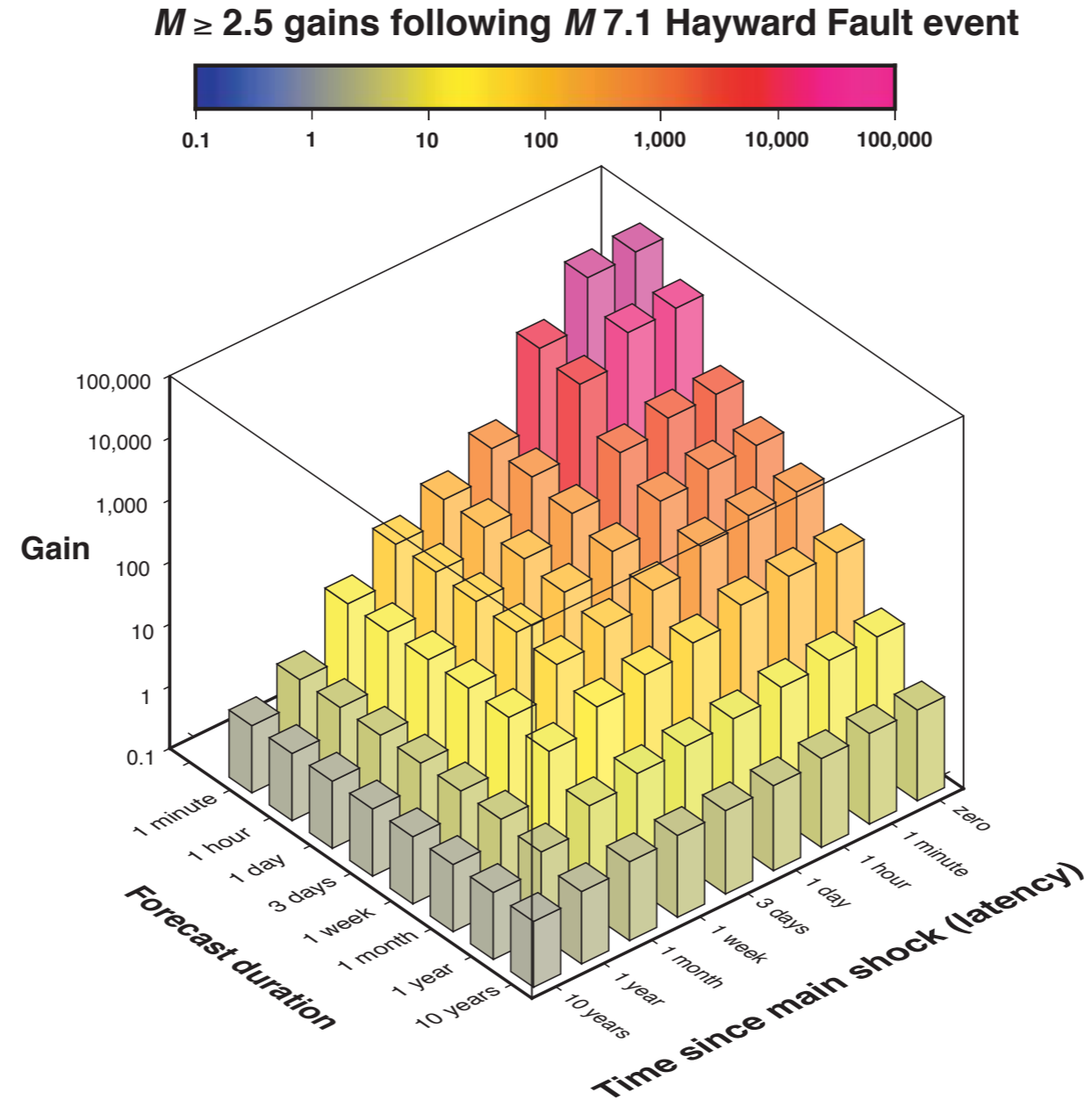
Moment rate functions all start out the same, which suggests the earthquake doesn't "know" its final size

What do changing earthquake probabilities look like in time?



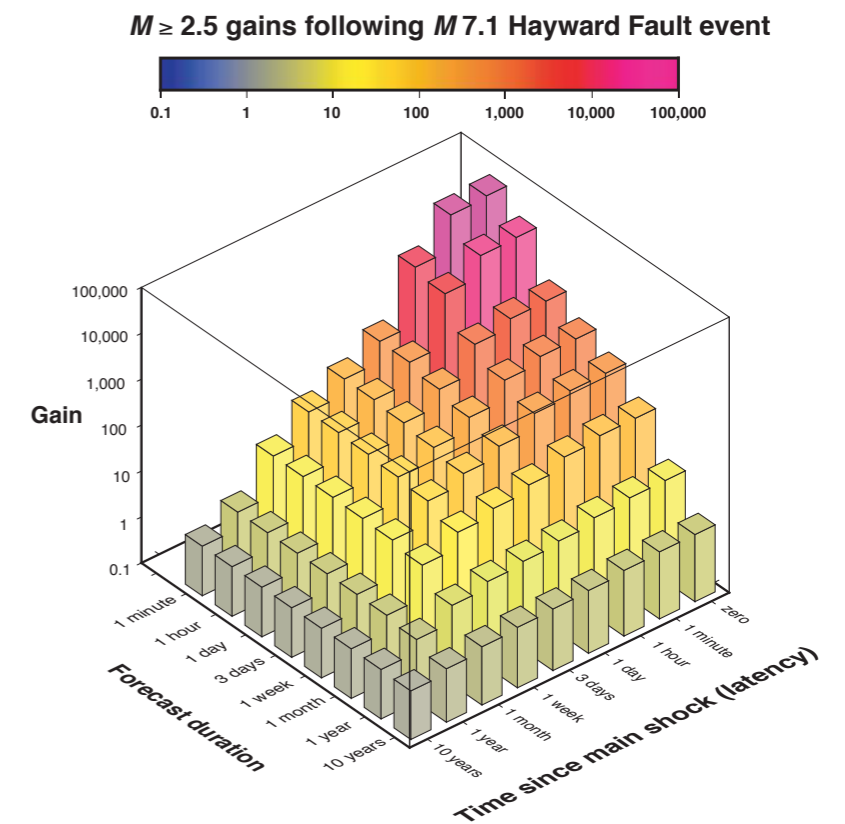
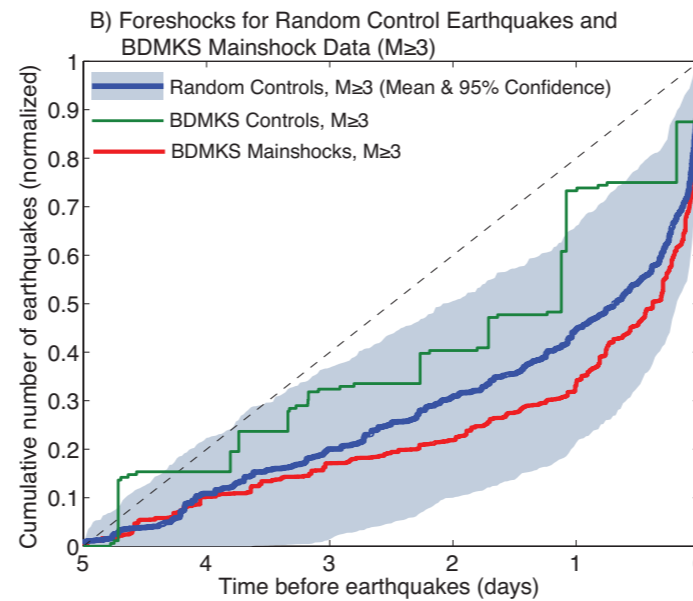
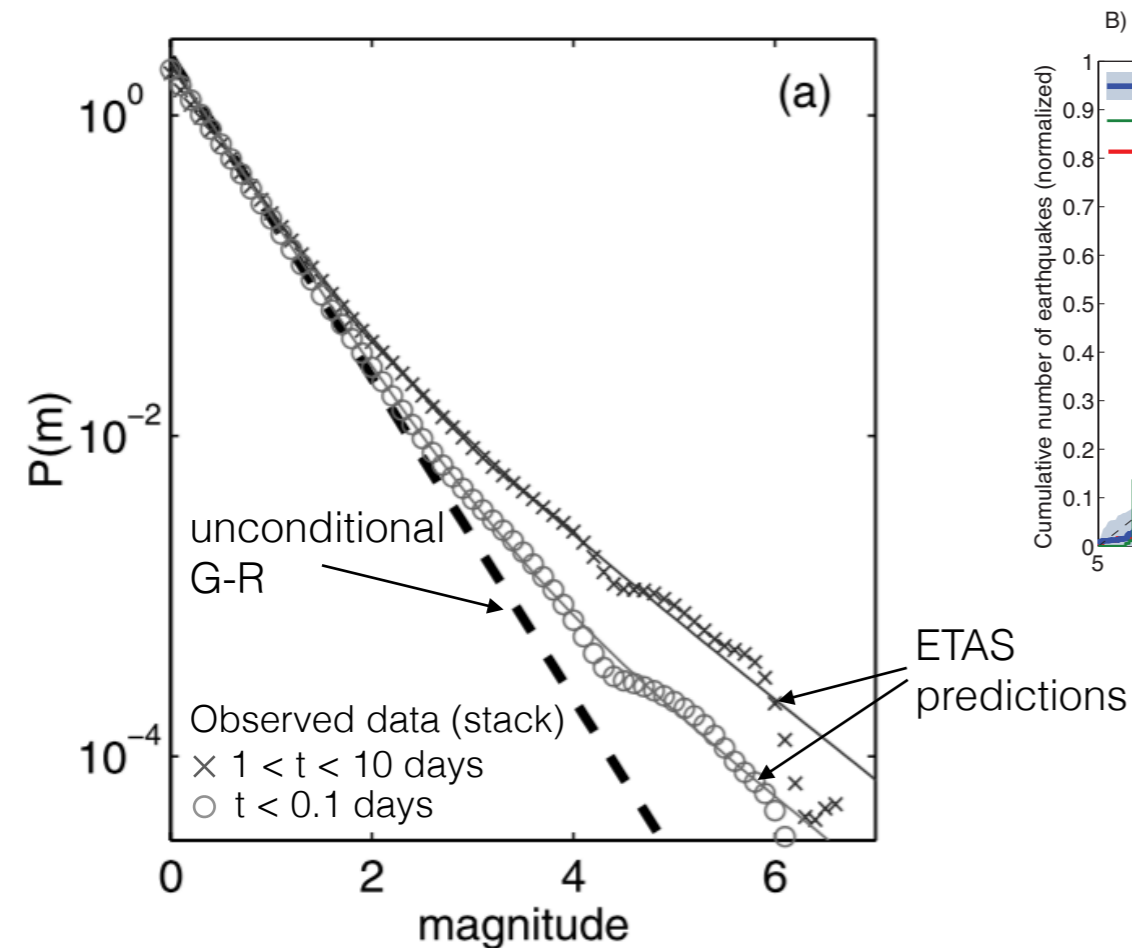
Even though foreshocks are not predictive of earthquake size, foreshock/ aftershock statistics can give orders of magnitude changes in the probabilities for future earthquakes of all sizes.

How big are the probability gains in ETAS?



Well-characterized scaling relations imply:

- b-value anomalies and inverse Omori acceleration for stacked foreshocks
- Probability gains of 100-1000 on time scales of a day



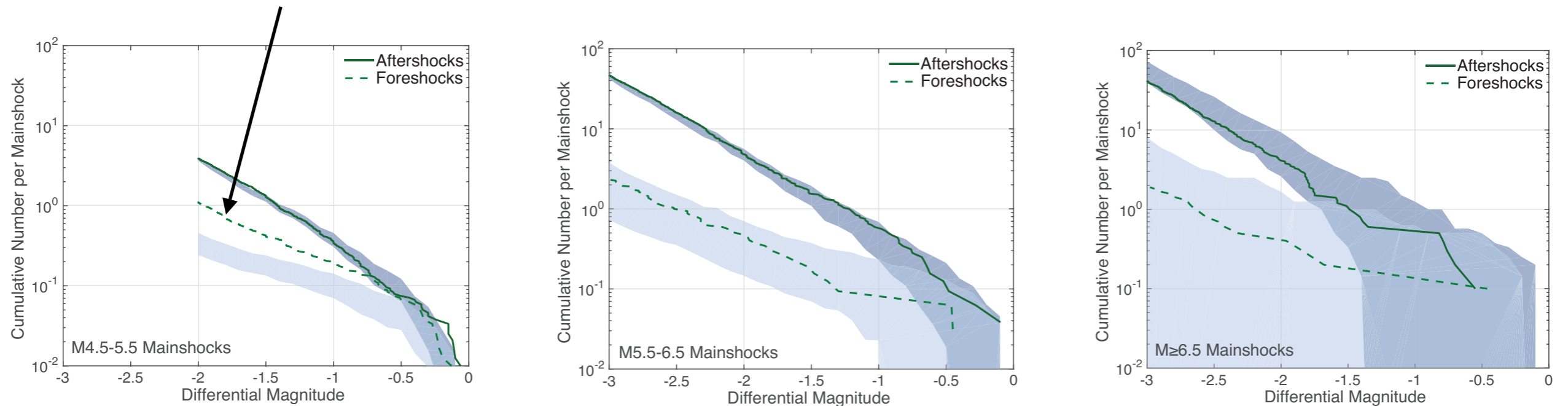
ETAS is an excellent null hypothesis that explains a large amount of the observed predictability in the data

Deviations from ETAS?

Foreshock and Aftershock Productivity as a Function of Differential Magnitude

As noticed by Brodsky (2011) and Shearer (2012), mainshocks in California have twice as many foreshocks as ETAS prediction

But this effect is only seen for smaller mainshocks!



Green lines show 28-year observed catalog in California

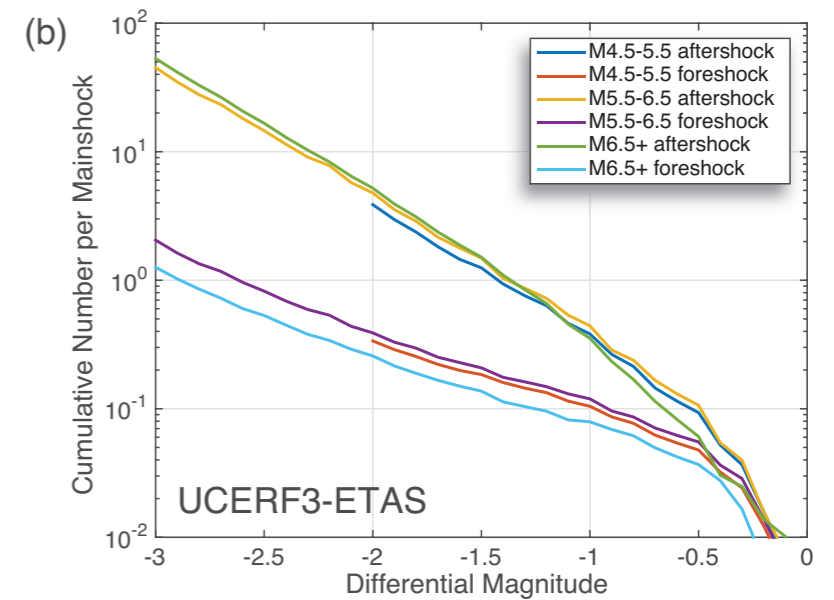
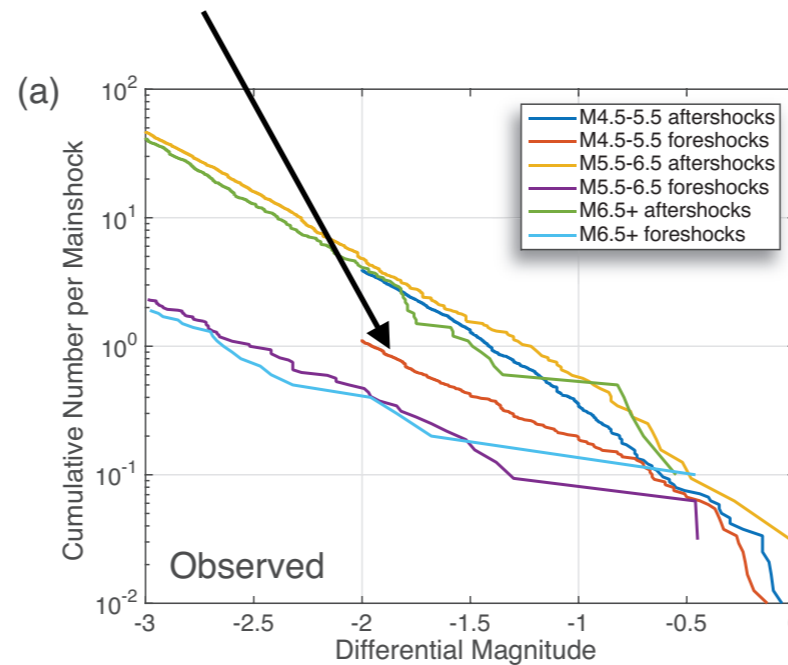
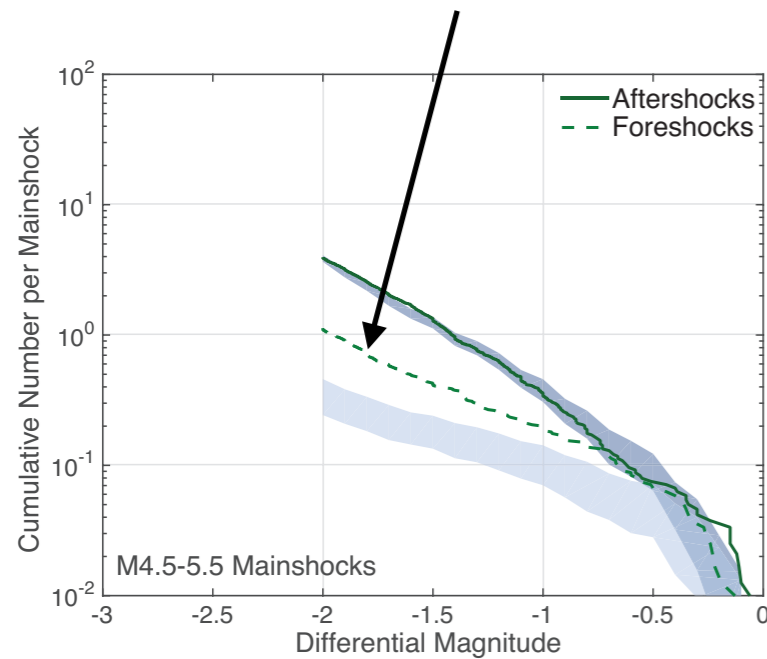
Blue shaded regions show range from 28-year UCERF3-ETAS snapshots

Deviations from ETAS?

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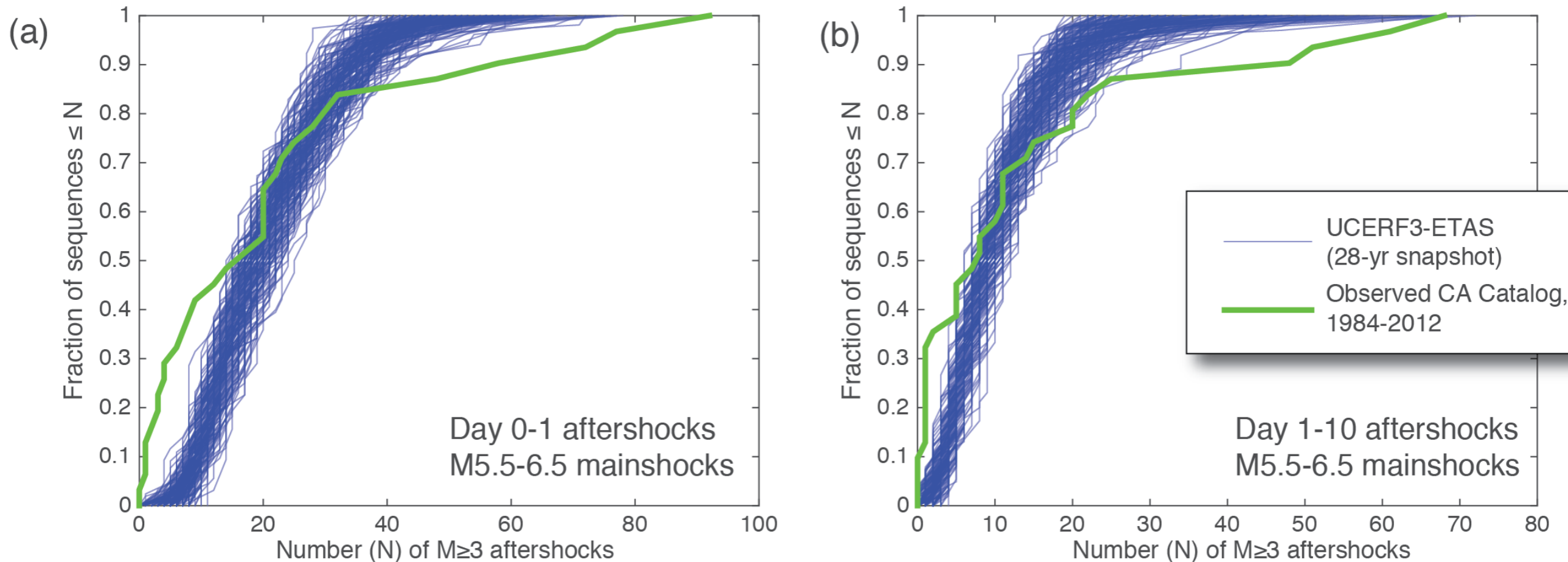
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Deviations from ETAS?

Inter-sequence Aftershock Productivity Variability

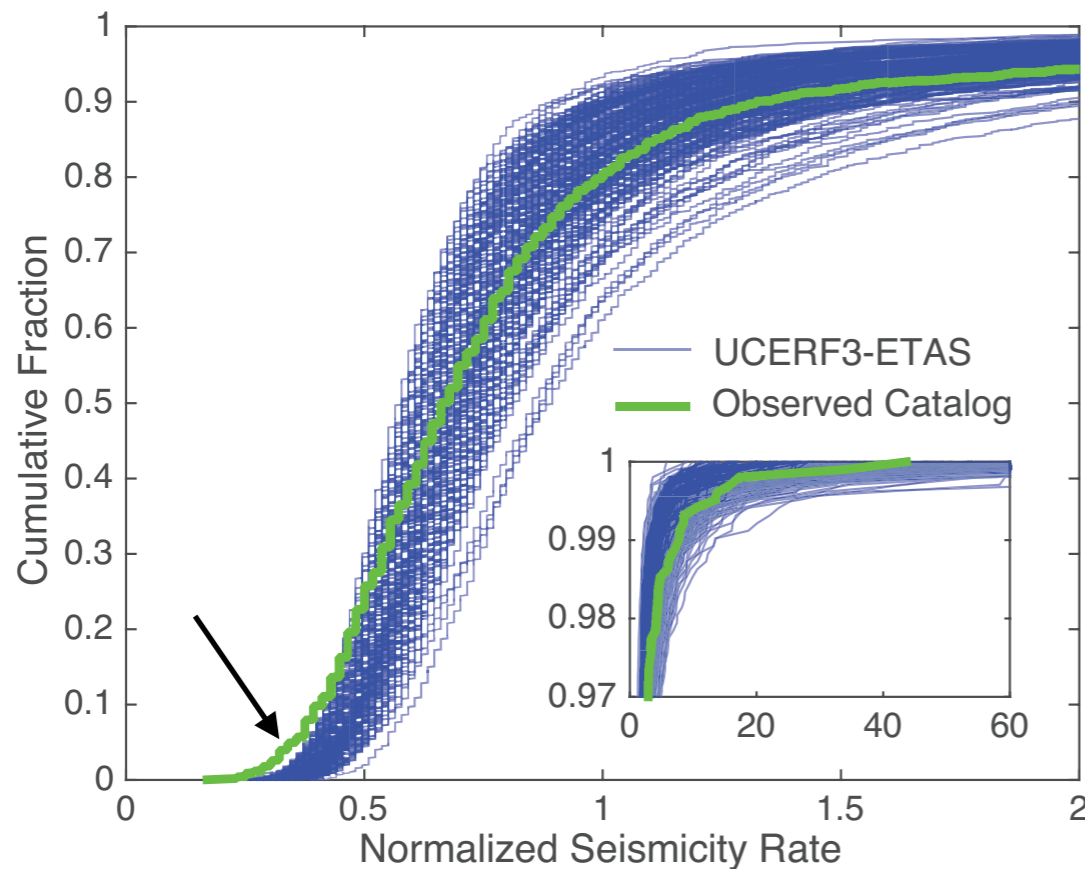


ETAS models that use one set of direct Omori parameters have less aftershock productivity variability than observed catalog

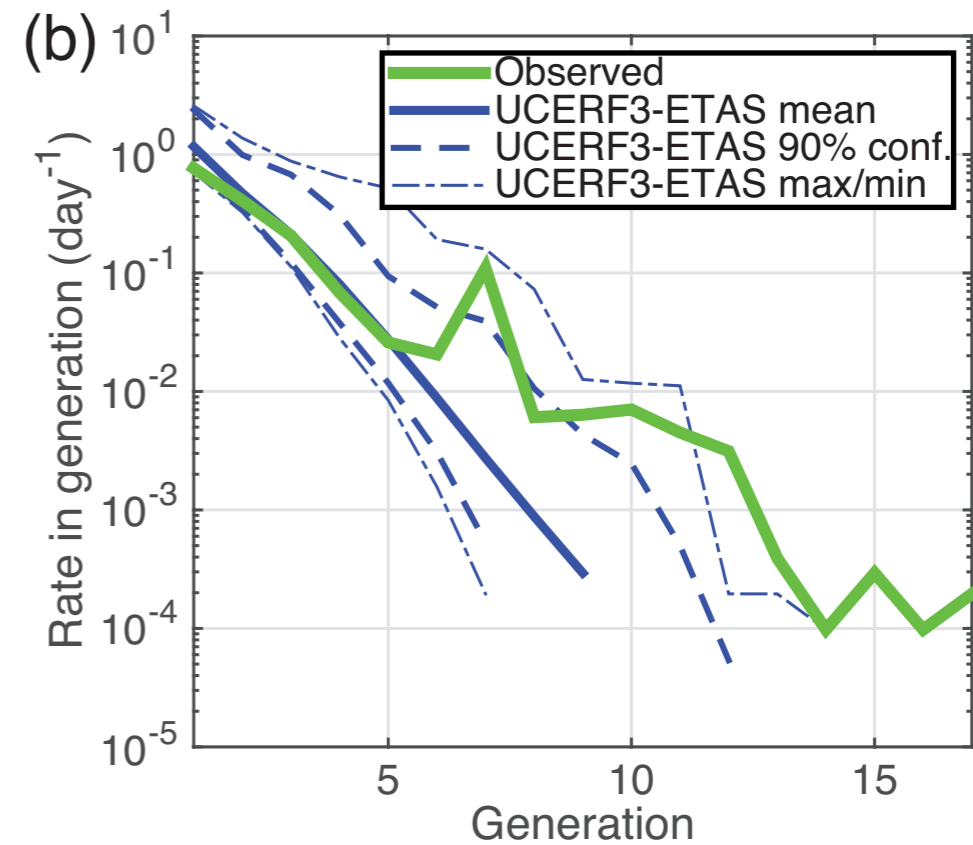
Deviations from ETAS?

Direct Omori parameters are likely close to critical (very little “background”)

Including the effect of “orphaned” aftershocks is important

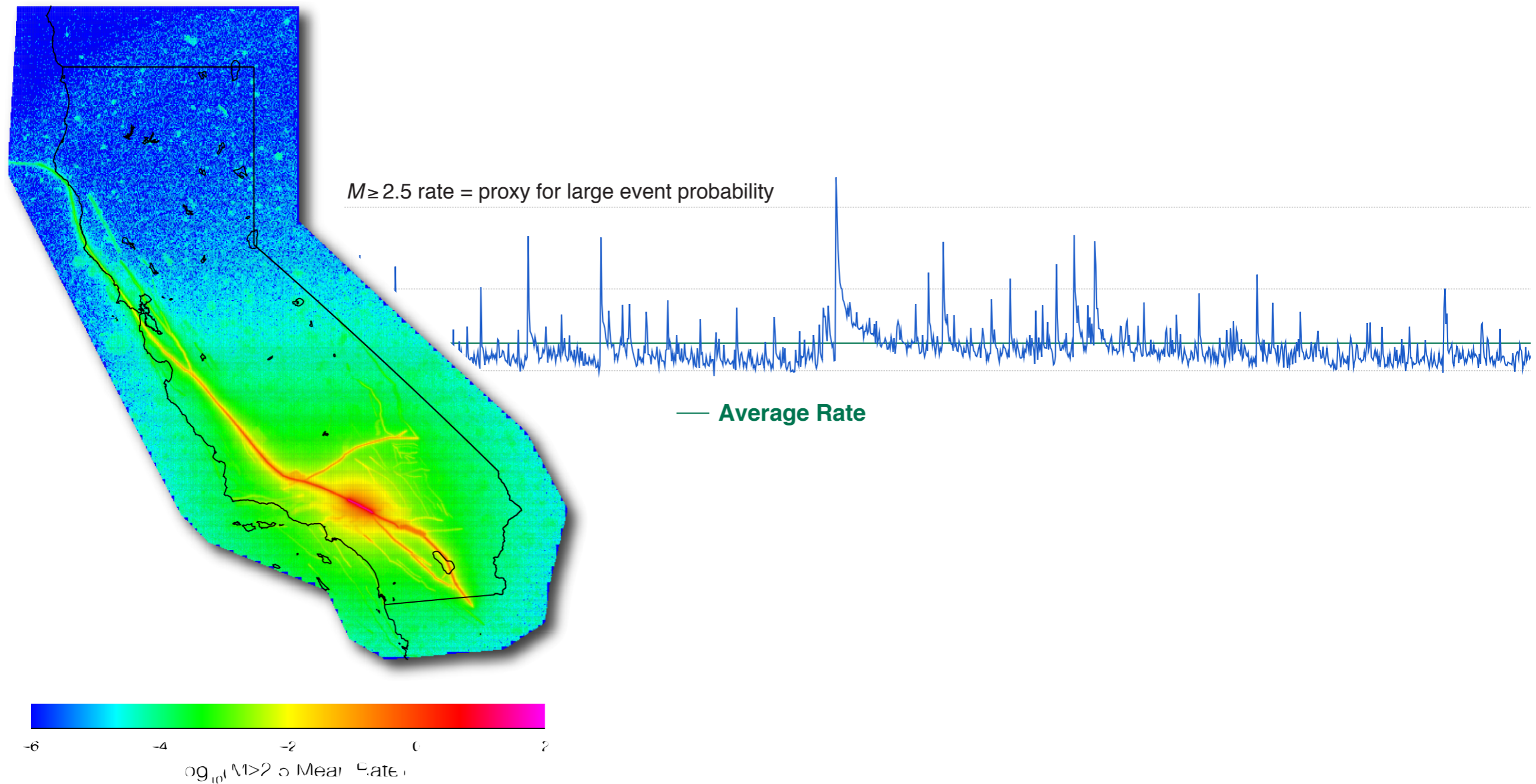


Real catalog (green) has more quiet periods



Real catalog (green) has more sequences that extend to higher generations

ETAS captures much of the predictability in seismicity



By better estimating parameters & modeling variations, we can further increase probability gains